

Nonlinear Effects of School Quality on House Prices

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We reexamine the relationship between quality of public schools and house prices and find it to be nonlinear. Unlike most studies in the literature, we find that the price premium parents must pay to buy a house in an area associated with a better school increases as school quality increases. This is true even after controlling for neighborhood characteristics, such as the racial composition of neighborhoods, which is also capitalized into house prices. In contrast to previous studies that use the boundary discontinuity approach, we find that the price premium from school quality remains substantially large, particularly for neighborhoods associated with high-quality schools. (JEL C21, I20, R21)

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The relationship between house prices and local public goods and services has been widely studied in the literature, dating back to Oates's (1969) seminal paper, in which he studied the effect of property tax rates and public school expenditures per pupil on house prices. Oates conjectured that if, according to the Tiebout (1956) model, individuals consider the quality of local public services in making locational decisions, an increase in expenditures per pupil should result in higher property values, whereas an increase in property tax rates would result in a decline in property values, holding other things equal across communities. Oates suggested that the variation in expenditures per pupil partially reflected the variation in the quality of public schools.

In the analysis of school quality, researchers have often applied the hedonic pricing model developed by Rosen (1974). In this model, the implicit price of a house is a function of its com-

parable characteristics, as well as measures of school quality and a set of neighborhood characteristics. A house's comparable characteristics include the number of bedrooms, square footage, and so on. The estimated coefficients from the regression represent the capitalization of the different components into house values.

In an influential study, Black (1999) argued that previous research estimating hedonic pricing functions introduced an upward bias from neighborhood quality effects that are unaccounted for in the data.¹ Specifically, she noted that better schools may be associated with better neighborhoods, which could independently contribute to higher house prices. Black circumvented this problem by estimating a linear hedonic pricing function using a restricted sample of data from

¹ By neighborhood *quality* we refer to the availability of mass transit and thoroughfares, proximity to commercial and industrial areas, and other such amenities, in addition to sociodemographic characteristics.

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houses along the boundaries of school attendance zones.² She rationalized that, while test scores make a discrete jump at attendance boundaries, changes in neighborhoods are smoother.³ The linear specification of the hedonic approach, including Black's (1999) variation, presupposes that the marginal valuation of below-average schools is equal to the valuation of above-average schools and results in a constant premium on school quality.⁴

In this paper, we argue that the relationship between school quality and house prices in the boundary discontinuity framework is better characterized as a *nonlinear* relationship. We formulate motivating hypotheses for the presence of nonlinear effects of school quality on house prices based on heterogeneous parent valuations of school quality and competition in the housing market. We then test for nonlinear effects estimating a nonlinear pricing function in the St. Louis, Missouri, metropolitan area, using standardized state math test scores as the measure of education quality. To control for neighborhood quality, we measure education capitalization by using Black's method of considering only houses located near attendance zone boundaries. We find that the effect of school quality is indeed best characterized as a nonlinear function.

We find, as did Black (1999), that controlling for unobserved neighborhood characteristics with boundary fixed effects reduces the premium estimates from test scores relative to the hedonic regression with the full sample of observations. We also find, however, that the linear specification for test scores underestimates the premium at high levels of school quality and overestimates the premium at low levels of school quality. In

contrast to Black (1999) and many subsequent studies in the literature, we find that the effects of school quality on housing prices remain substantially large even after controlling for neighborhood demographics, such as the racial composition of neighborhoods, in addition to boundary fixed effects. We also find that the racial composition of neighborhoods has a statistically significant effect on house prices.

This paper is organized as follows. The next section presents a survey of the recent literature. We then describe the hypotheses and the econometric model. Our data description is followed by the empirical results.

LITERATURE REVIEW

Ross and Yinger (1999) and Gibbons and Machin (2008) provide surveys of the literature on capitalization of local public goods and services. Examples of the traditional full-sample hedonic regression approach include papers by Haurin and Brasington (1996), Bogart and Cromwell (1997), Hayes and Taylor (1996), Weimer and Wolkoff (2001), and Cheshire and Sheppard (2002). Additional works are surveyed in Sheppard (1999).

Various studies in the hedonic analysis tradition have used so-called input-based measures of education quality, such as per-pupil spending. Hanushek (1986, 1997) found that school inputs have no apparent impact on student achievement and are therefore inappropriate as measures of school quality. His insights have led to the more prevalent use of *output-based* measures, such as standardized test scores.⁵ The research on education production functions also has made the case that *value-added* measures of achievement—often measured as the marginal improvement in a particular cohort's performance over a period of time—would be more appropriate as measures of quality in capitalization studies. However, con-

² A school's attendance zone delimits the geographic area around the public school the residents' children would attend. In this text, we often refer interchangeably to a school's attendance zone as the *school*, but this term should not be confused with *school district*, which is an administrative unit in the public school system often comprising several schools.

³ Black's (1999) boundary discontinuity approach is part of the more general *regression discontinuity design* surveyed by Imbens and Lemieux (2008).

⁴ Nonlinear effects are nevertheless routinely allowed among some house characteristics, such as the number of bathrooms and the age of the building.

⁵ Some authors, however, have expressed concerns about the potential endogeneity of school quality when it is measured by indicators of student performance. Gibbons and Machin (2003), for example, argue that better school performance in neighborhoods with high house prices may reflect that wealthy parents buy bigger houses with more amenities and therefore devote more resources to their children.

structuring value-added measures requires tracking groups of students over time and implies more sophistication in the decisionmaking process of potential buyers, as value-added measures are not commonly available to the public. Brasington (1999), Downes and Zabel (2002), and Brasington and Haurin (2006) found little support for using value-added school quality measures in the capitalization model; they argued that home buyers favor, in contrast, more traditional measures of school quality in their housing valuations.

A prevalent concern of capitalization studies is the possibility of omitted variable bias, induced by failing to account for the correlation between school quality and unobserved neighborhood characteristics, as better schools tend to be located in better neighborhoods. As mentioned previously, Black (1999) tackled this problem by restricting the sample to houses near the boundaries between school attendance zones and controlling for neighborhood characteristics with boundary fixed effects. A rudimentary precursor of this idea was analyzed by Gill (1983), who studied a sample of houses in Columbus, Ohio, restricting observations to neighborhoods with similar characteristics. Also, Cushing (1984) analyzed house price differentials between adjacent blocks at the border of two jurisdictions in the Detroit, Michigan, metropolitan area. Recent examples of this approach include studies by Leech and Campos (2003), Kane, Staiger, and Samms (2003), Kane, Staiger, and Riegg (2005), Gibbons and Machin (2003, 2006), Fack and Grenet (2007), and Davidoff and Leigh (2007).

The boundary discontinuity approach has been criticized in some recent studies motivated primarily by concerns about the successful removal of any remaining omitted spatial fixed effects (Cheshire and Sheppard, 2004) or the possibility of discontinuous changes in neighborhood characteristics, which also depends on the definition of “neighborhood” that is adopted (Kane, Staiger, and Riegg, 2003; Bayer, Ferreira, and McMillan, 2007). However, barring the availability of repeat sales data or information on boundary redistricting or policy changes to supply the exogenous variation required for identification, in the case of stable boundary definitions and cross-

sectional data, the boundary discontinuity approach remains a useful methodology. In addition to boundary discontinuities, recent studies have used various methods of addressing the omitted variables and endogeneity issues, including time variation (Bogart and Cromwell, 2000; Downes and Zabel, 2002; Figlio and Lucas, 2004; Reback, 2005, among others), natural experiments (Bogart and Cromwell, 2000, and Kane, Staiger, and Riegg, 2005), spatial statistics (Gibbons and Machin, 2003, and Brasington and Haurin, 2006), or instrumental variables (Rosenthal, 2003, and Bayer, Ferreira, and McMillan, 2007).

In this paper, we measure school quality at the individual school level and we regress house prices on their physical characteristics and a full set of pairwise boundary dummies to control for unobserved neighborhood characteristics. Additionally, in response to the criticisms of the boundary discontinuity approach, we augment the estimation by controlling for a set of demographic characteristics defined at the Census-block level (as opposed to the larger block groups or tracts). Many papers that do not use the boundary discontinuity approach measure education quality at the school-district level, as opposed to considering schools individually. These studies also face the challenge of devising appropriate definitions of neighborhoods to match the geographic level at which school quality is measured. For example, Clapp, Nanda, and Ross (2008) measure school quality at the school-district level and use Census-tract fixed effects to control for omitted neighborhood characteristics. Brasington and Haurin (2006) also measure school quality at the school-district level but use spatial statistics rather than fixed effects to control for neighborhood characteristics.

To the best of our knowledge, nonlinear hedonics from school quality have been explored only by Cheshire and Sheppard (2004) in a study of primary and secondary schools in the United Kingdom. They estimate a full-sample, standard hedonic regression modified to include Box-Cox transformations of house prices, house characteristics, and measures of school quality. Their evidence suggests that the price-quality relationship is highly nonlinear. Although Cheshire and

Sheppard include a wide variety of local neighborhood characteristics as controls, their approach also suffers from the possibility of omitted variable bias present in traditional hedonic models.

A previous study of house prices in the St. Louis metropolitan area by Ridker and Henning (1967) found no evidence of education capitalization in St. Louis house prices. Although their main concern was to determine the negative effect of air pollution on housing prices, they included a dummy variable that indicated residents' attitudes about the quality of the schools (above average, average, and below average). Ridker and Henning (1967) acknowledged, however, that their study may suffer from small-sample bias that could explain this seemingly contradictory finding. Kain and Quigley (1970) also conducted an early study of the components of a hedonic price index for housing in the St. Louis metropolitan area, but it does not consider measures of school quality.

THE MODEL

In this section, we discuss three motivating hypotheses that can generate nonlinear effects from school quality on house prices. We argue that the nonlinearity with respect to school quality illustrates two aspects of the market for public education that are reflected in the housing market. Although developing a full theoretical model is beyond the scope of our paper, interested readers are referred to a previous working paper version in which we sketch a search model of the housing market in the spirit of Wheaton (1990) and Williams (1995) that can motivate these features.

Three Arguments for Nonlinear Effects

First, in an environment in which potential buyers are heterogeneous in the intensity of their preferences for school quality and neighborhood characteristics, buyers with a stronger preference for education quality may concentrate their buying search for a house in the highest-quality attendance zones. As school quality increases, competition from other buyers creates an increasingly tight housing market, because the housing supply in these areas is often very inelastic, as

most metropolitan areas have a fixed housing stock in the short run.

This argument is similar to that proposed by Hilber and Mayer (2009). They argue that scarcity of land confounds identification of the education premium. Brasington (2002) and Hilber and Mayer (2009) have also noted that the extent of capitalization in a hedonic framework may vary depending on whether houses are located near the interior or the edge of an urban area. They find that capitalization is weaker toward the edge, where housing supply elasticities and developer activity are greater.

Second, alternative schooling arrangements (e.g., private schools, home schooling, magnet schools) can provide home buyers with high-quality education even if they choose to live in lower-quality public school attendance zones, allowing for a reduced price premium in these neighborhoods. The existence of these options underlies our belief that a constant premium across the range of school quality is not realistic.

The previous two hypotheses rely on the heterogeneity of preferences for school quality and neighborhood characteristics among the population of prospective home buyers, a feature widely documented in the literature. Bayer, Ferreira, and McMillan (2007), for example, argue that there is a considerable degree of heterogeneity in homeowners' preferences for schools and racial composition of neighborhoods.

Finally, an alternative hypothesis that can generate nonlinearities is that school quality can be considered a luxury good; therefore, at higher-quality schools (and therefore richer neighborhoods), people would be willing to pay more for the same marginal increase in school quality.

The Econometric Model

We now estimate a model of house prices. Specifically, we estimate the dollar value difference in home prices for a quantified increase in school quality. We discuss three alternative specifications that include two different identification techniques to disentangle neighborhood quality from school quality.

Pure Hedonic Pricing Model. As a benchmark, we introduce a hedonic pricing equation

in which the sale price is described as a function of the characteristics of the house and its location-specific attributes, including the quality of the school associated with it. The basic hedonic function can be described as follows:

$$(1) \quad \ln(p_{iaj}) = \kappa + \mathbf{X}'_i \boldsymbol{\beta} + \mathbf{Z}'_j \boldsymbol{\delta} + \mu_a \psi^H + \varepsilon_{iaj},$$

where p_{iaj} is the price of house i in attendance zone a in neighborhood j . The vector \mathbf{X}_i represents the comparable aspects of house i (e.g., the number of bedrooms, bathrooms, and so on) and vector \mathbf{Z}_j represents local characteristics. The value μ_a is the quality of the school in attendance zone a . In this paper, we measure school quality with an index constructed from test scores, defined at the school level and expressed in standard deviations (SDs) from the mean. The quantity of interest ψ^H is the education capitalization premium and represents the percentage increment in house prices from increasing school test scores by 1 SD.

Thus, the house price reflects all relevant attributes; that is, the physical and location-specific characteristics of the home are capitalized into the house value even if they are not directly consumable by the current tenants (because of their effects on the resale value of the house).⁶ One potential problem with this specification is that the comparable house characteristics, \mathbf{X}_i , do not fully capture the quality of the house (updates, condition, landscaping, layout, and so on), the quality of the surrounding neighborhood, and various other factors. The hedonic pricing function attempts to capture these factors with the inclusion of the \mathbf{Z}_j vector. The success with which the model captures these unobserved factors often depends on how coarsely the geographic area encompassed by \mathbf{Z}_j is defined (i.e., for how small a vicinity around the house \mathbf{Z}_j provides variation).

Linear Boundary Fixed Effects Model. As discussed earlier, the methodology of adding the location characteristics vector, \mathbf{Z}_j , may reduce but not entirely account for all of the variation that can be introduced on a neighborhood level. Suppose that the neighborhood characteristics

gradient is large in absolute value. This implies that houses a few blocks away from each other can vary a great deal in “atmosphere” and, therefore, in price. This variation can be related to distance to amenities, mass transit, and thoroughfares (i.e., highway access), proximity to commercial and industrial zoning, single-family housing density, and so on. The vector \mathbf{Z}_j may be unable to account for all the unobserved neighborhood variation that confounds the estimate of the capitalization premium because of the potential correlation with school quality. Much of this variation (though admittedly not all) can be corrected for by analyzing houses that are geographically close.

The boundary discontinuities refinement considers only houses that are geographically close to school attendance zone boundaries and replaces the vector of local characteristics with a full set of pairwise boundary dummies. Each house in this reduced sample is associated with the nearest, and hence unique, attendance zone boundary. This yields the following:

$$(2) \quad \ln(p_{iab}) = \kappa + \mathbf{X}'_i \boldsymbol{\beta} + \mathbf{K}'_b \boldsymbol{\phi} + \mu_a \psi^L + \varepsilon_{iab},$$

where \mathbf{K}_b is the vector of boundary dummies and the subscript b indexes the set of boundaries. The resulting education premium calculated with the linear boundary fixed effects model is ψ^L . Equation (2), then, is equivalent to calculating differences in house prices on opposite sides of attendance boundaries while controlling for house characteristics and relating the premium to test-score information.

The boundary dummies allow us to account for unobserved neighborhood characteristics of houses on either side of an attendance boundary because two homes next to each other generally would have the same atmosphere. For this approach to be successful, particular care must be taken to exclude from the sample attendance zones whose boundaries coincide with administrative boundaries, rivers, parks, highways, or other landmarks that clearly divide neighborhoods, as neighborhood characteristics in these cases would be expected to vary discontinuously at the boundary.

⁶ For example, if the current tenants have no school-aged children.

Nonlinear Boundary Fixed Effects Models.

As an alternative to the linear model, we consider the possibility that the capitalization premium is not constant over the range of school qualities. This is accomplished by testing whether the education capitalization term enters nonlinearly. Consider the following pricing equation:

$$(3) \quad \ln(p_{iab}) = \kappa + \mathbf{X}'_i\boldsymbol{\beta} + \mathbf{K}'_b\boldsymbol{\phi} + f(\mu_a) + \varepsilon_{iab},$$

where $f(\mu_a)$ represents a potentially nonlinear function of school quality. For simplicity, suppose the function $f(\mu_a)$ is composed of a linear polynomial term and higher-order polynomial terms in school quality. That is,

$$(4) \quad f(\mu_a) = \psi_1\mu_a + \psi_2\mu_a^2 + \psi_3\mu_a^3,$$

where ψ_m , $m = 1, 2, 3$, are scalar parameters. We then rewrite equation (3) as

$$(5) \quad \ln(p_{iab}) = \kappa + \mathbf{X}'_i\boldsymbol{\beta} + \mathbf{K}'_b\boldsymbol{\phi} + \psi_1\mu_a + \psi_2\mu_a^2 + \psi_3\mu_a^3 + \varepsilon_{iab}.$$

Specification (5) offers several advantages over the linear form (equation (2)). First, the rate at which the nominal premium varies across the range of school quality is not fixed. This allows us to differentiate the incremental effects on house prices of low- versus high-quality school attendance zones. Second, with a constant premium the linear model *penalizes* houses in low-quality school attendance zones by valuing them below what would be predicted by their comparable attributes.⁷ Moreover, the penalty increases as the school quality worsens. This scenario is unappealing because, as mentioned before, potential buyers who value education quality often can find substitute arrangements outside the public school system. Our prediction is that houses in lower-quality attendance zones command a smaller premium; in other words, the price function should be flatter for areas with lower test scores and steeper for those with higher test scores. This possibility is explicitly excluded in the linear model.

⁷ We adopt the convention that an increase in school quality induces a *premium* on house prices, whereas a decrease in school quality imposes a *penalty* on house prices.

A Note on the Estimation. We estimated regression equations (1), (2), and (5) with ordinary least squares. In all cases, we computed robust standard errors (SEs) clustered at the school level. For completeness, the “Results” section also presents the estimation of the nonlinear models using the full sample. We included boundary dummies in the regression equation and estimated the coefficients for these variables directly.

In an attempt to reduce any remaining bias from omitted characteristics, some recent studies, such as that by Bayer, Ferreira, and McMillan (2007), have supplemented their analysis by including demographic controls in the regressions. We therefore present results of the boundary fixed effects regressions in which the vector \mathbf{Z}_i of neighborhood characteristics has been reinserted in the estimation. In particular, we control for the racial composition of neighborhoods. Studies that specifically consider the racial composition of neighborhoods include those by Bogart and Cromwell (2000), Downes and Zabel (2002), Cheshire and Sheppard (2004), Kane, Staiger, and Riegg (2005), Reback (2005), Clapp, Nanda, and Ross (2007), and Bayer, Ferreira, and McMillan (2007).

DATA

In this analysis, we restrict our attention to single-family residences and elementary school attendance zones. Each observation corresponds to a house and is described by variables reflecting its physical characteristics, the quality of the local public elementary school that children in the household would attend, and the characteristics of the neighborhood in which the house is located—namely, demographic indicators measured at the Census-block level and property tax rates measured at the school-district level.

Real Estate Prices and Housing Characteristics

We obtained house price and house characteristics data from First American Real Estate Solutions. The observations selected correspond to a cross section of single-family residences sold during the 1998-2001 period in the St. Louis,

Missouri, metropolitan area. The data are from transactions as recorded in county property records. After eliminating from the original dataset observations with missing or outlier house prices (outside a bound of 3.5 SDs from the mean unadjusted house price), our sample includes 38,656 single-family residences.

We deflated house prices to 1998 dollars with the Office of Federal Housing Enterprise Oversight repeat-sales price index for the entire St. Louis metropolitan area.⁸ In the full sample the resulting adjusted house price has a mean of \$148,082 and an SD of \$161,397. House characteristics include the total number of rooms, number of bedrooms, number of bathrooms, lot size, internal square footage, age of the structure, and number of stories in the house.

Attendance Zones

For the boundary discontinuity analysis, we obtained the definitions of 121 attendance zones for elementary schools in 15 school districts in St. Louis County. Most of these were obtained by contacting the school districts directly. Boundaries were variously provided as listings of streets, maps, and in some isolated cases as geocoded files. We, in turn, geocoded all the attendance zones and determined the boundary for every pair of adjacent schools, as in Black's paper (1999). We also geocoded each house in our sample using the street address. We then selected houses within a 0.1-mile buffer of the boundaries and assigned them to the nearest (and therefore unique) pairwise boundary.⁹ We also eliminated from the boundary sample observations in St. Louis County that were associated with the boundaries of St. Louis City schools because the City property records contained no house price information. The final boundary sample consisted of 10,190 single-family residences.

⁸ House prices were deflated using the average price index corresponding to the quarter of the sale. The results were qualitatively unaffected if the National Association of Realtors price index was used instead.

⁹ Black considers a number of different boundary width ranges and finds no significant differences. Our sample does not permit wider boundaries as these would encompass some attendance zones almost entirely.

Neighborhood Characteristics

Houses were also matched to Census blocks as the geographic unit at which we measured neighborhood demographics. We used the publicly available population tables at the block level from the Census 2000 Summary File 1, which includes counts by age, sex, and race, to construct the following measures: percent of females, percent of school-aged children (between 5 and 14 years of age), and percent of nonwhite population (defined as the total population count minus the count of white people).¹⁰

Additionally, we include as neighborhood controls the property tax rates defined at the school-district level for the years 1998 through 2001. In this case, each house was matched to the tax rate prevailing during the year of sale in its associated school district.¹¹ Table 1 presents summary statistics for house prices and characteristics with neighborhood characteristics for both the full and boundary samples.

Test Scores

As the measure of school quality, we use a school-level index generated by the Missouri Department of Elementary and Secondary Education. This index is computed from test score data from the Missouri Assessment Program (MAP); annual MAP testing is a statewide mandate for public schools. The MAP test includes a *Mathematics* section, a *Communication Arts* section (which includes a *Reading* portion), a *Science* section, and a *Social Studies* section.

Neither individual student scores nor school-level averages of these scores are publicly available. Instead, for each content area, the publicly available data provide the overall school-level MAP index. This index is obtained with a state-defined formula as the weighted sum of the percentages of students in each of five performance categories (Advanced, Proficient, Nearing

¹⁰ Our choice of demographic variables was limited by the availability of information at the block level in the public data files. Alternative measures such as median household income or share of households with a female head of household are not available at the block level.

¹¹ The analysis was not affected qualitatively if an average over the period was used instead.

Table 1**Summary Statistics (House and Neighborhood Characteristics)**

House variables	Full sample (N = 38,656)		Boundary sample (N = 10,190)	
	Mean	SD	Mean	SD
Sale price (1998 US\$)	148,081.67	161,397.24	142,033.42	176,191.20
Log of sale price	11.62	0.73	11.56	0.75
Number of bedrooms	2.96	0.84	2.9	0.84
Number of bathrooms	2.01	0.95	1.95	0.93
Number of bathrooms (squared)	4.97	5.05	4.66	5.04
Age of building	38.91	20.63	40.72	21.27
Age of building (squared)	1,939.38	1,922.87	2,110.15	2,028.41
Lot area (1,000s of sq. ft.)	14.75	38.35	13.61	39.20
Living area (1,000s of sq. ft.)	1.16	0.44	1.13	0.42
Number of stories	1.24	0.42	1.23	0.41
Total number of rooms	6.38	1.6	6.26	1.57

Census variables	Full sample (N = 6,360 blocks)		Boundary sample (N = 2,560 blocks)	
	Mean	SD	Mean	SD
Percent female population	51.17	11.22	51.34	11.33
Percent nonwhite population	20.43	29.29	22.42	30.67
Percent population 5 to 14 years of age	9.34	9.58	9.98	9.38

Table 2**Summary Statistics (Test Scores and Property Tax)**

Variable	Mean	SD	Minimum	Maximum
Test scores (N = 121 schools)				
Math MAP score	211.45	19.44	168.14	250.18
Science MAP score	211.88	22.56	100.00	242.61
Reading MAP score	200.73	20.15	100.00	228.94
Property tax (N = 15 school districts)				
Property tax rate (\$1/\$1,000 of assessed house value)	4.23	0.91	2.60	5.74

Table 3
Correlation Table

Variable	Log house price	Math score	Math score (squared)	Math score (cubed)	Number of bedrooms	Number of bathrooms	Number of bathrooms (squared)	Age of building	Age of building (squared)	Lot area (1,000s of sq. ft.)	Living area (1,000s of sq. ft.)	Number of stories	Number of rooms	Census block: Percent female	Census block: Percent nonwhite	Census block: Percent people 5 to 14 years of age	Property tax rate
Log house price	1.00																
Math score	0.66	1.00															
Math score (squared)	-0.14	-0.35	1.00														
Math score (cubed)	0.50	0.87	-0.44	1.00													
Number of bedrooms	0.57	0.34	-0.09	0.25	1.00												
Number of bathrooms	0.68	0.50	-0.07	0.37	0.64	1.00											
Number of bathrooms (squared)	0.63	0.43	-0.01	0.32	0.58	0.94	1.00										
Age of building	-0.32	-0.38	0.17	-0.27	-0.29	-0.48	-0.39	1.00									
Age of building (squared)	-0.21	-0.29	0.16	-0.21	-0.21	-0.36	-0.28	0.94	1.00								
Lot area (1,000s of sq. ft.)	0.23	0.13	0.02	0.10	0.14	0.17	0.19	-0.03	-0.01	1.00							
Living area (1,000s of sq. ft.)	0.51	0.36	-0.04	0.26	0.39	0.45	0.43	-0.30	-0.27	0.20	1.00						
Number of stories	0.46	0.31	-0.02	0.22	0.47	0.56	0.52	-0.21	-0.07	0.06	-0.13	1.00					
Number of rooms	0.65	0.37	-0.04	0.26	0.82	0.71	0.67	-0.22	-0.14	-0.18	0.47	0.49	1.00				
Census block: Percent female	-0.11	-0.09	0.05	-0.07	0.11	-0.09	-0.08	0.04	0.02	-0.07	-0.08	-0.04	-0.11	1.00			
Census block: Percent nonwhite	-0.49	-0.69	0.48	-0.60	-0.25	-0.35	-0.28	0.30	0.24	-0.09	-0.24	-0.21	-0.26	0.16	1.00		
Census block: Percent people 5-14 yrs. of age	0.01	-0.07	0.12	-0.07	0.14	0.08	0.08	-0.13	-0.09	0.02	0.03	0.09	0.11	0.04	0.17	1.00	
Property tax rate	-0.47	-0.68	0.26	-0.56	-0.20	-0.35	-0.29	0.27	0.25	-0.07	-0.29	-0.14	-0.22	0.05	0.56	0.14	1.00

Table 4
Education Regressions: Full Sample

Variable	Log house price		
	(1)	(2)	(3)
Math score	0.21734*** (7.79)	0.22192*** (7.13)	0.31693*** (7.70)
Math score (squared)		0.03002 (1.48)	0.01555 (0.76)
Math score (cubed)			-0.03606** (-2.60)
Number of bedrooms	0.01062 (1.09)	0.01502 (1.52)	0.01575 (1.62)
Number of bathrooms	0.14086*** (4.75)	0.14413*** (4.93)	0.13458*** (4.44)
Number of bathrooms (squared)	-0.00612 (-1.14)	-0.00740 (-1.37)	-0.00501 (-0.89)
Age of building	0.00065 (0.37)	0.00057 (0.31)	0.00123 (0.67)
Age of building (squared)	0.00002 (1.35)	0.00002 (1.31)	0.00002 (1.03)
Lot area (1,000s of sq. ft.)	0.00123*** (4.21)	0.00120*** (4.27)	0.00119*** (4.17)
Living area (1,000s of sq. ft.)	0.45365*** (20.02)	0.44475*** (17.35)	0.43526*** (19.05)
Number of stories	0.39693*** (11.29)	0.38775*** (10.58)	0.37835*** (10.87)
Number of rooms	0.07484*** (10.10)	0.07421*** (10.21)	0.07245*** (10.11)
Census block: Percent female	-0.00061 (-0.88)	-0.00050 (-0.73)	-0.00053 (-0.79)
Census block: Percent nonwhite	-0.00221*** (-3.62)	0.00277*** (5.06)	-0.00257*** (-4.57)
Census block: Percent people 5 to 14 years of age	-0.00017 (-0.19)	-0.00033 (-0.38)	-0.00021 (-0.24)
Property tax rate	-0.04636 (-1.65)	-0.04457 (-1.51)	-0.03562 (-1.28)
Constant	10.00143*** (59.89)	9.99065*** (57.55)	9.96337*** (58.13)
<i>N</i>	38,656	38,656	38,656
<i>R</i> ²	0.697	0.699	0.702
Adjusted <i>R</i> ²	0.697	0.698	0.702

NOTE: *t*-Statistics are listed in parentheses. ***Significant at the 1 percent level.

Proficient, Progressing, and Step 1). The formula is MAP index = (percent in Step 1) \times 1 + (percent in Progressing) \times 1.5 + (percent in Nearing Proficient) \times 2 + (percent in Proficient) \times 2.5 + (percent in Advanced) \times 3. The weights are exogenously determined by the Missouri Department of Elementary and Secondary Education.¹²

For our study we chose the math MAP index for elementary schools only (fourth grade) as our measure of school quality.¹³ This measure was then averaged over the 1998-2001 period to remove any year-to-year noise in the component variables (as in Bayer, Ferreira, and McMillan, 2007). Because our housing data are essentially cross sectional, this procedure provides one consistent score for each school in the sample.

Table 2 presents summary statistics for MAP indices along with property tax rates among the schools and school districts included in the sample. Table 3 presents the correlation matrix for the variables used in the analysis.

EMPIRICAL RESULTS

Standard Hedonic Regression

Table 4 presents the regression results using the full sample, which includes neighborhood demographic controls but excludes the boundary fixed effects. In addition to the traditional linear model, we include the quadratic and cubic specifications in test scores for completeness.

The housing characteristics enter the pricing equation with the expected sign. Increases in living area, lot size, and the total number of rooms increase the price of a house on average. Similarly, the number of bathrooms and the number of stories have a positive and statistically significant effect. The number of bedrooms, the number of bathrooms squared, the age of the building, and

its square do not seem to have a statistically significant effect in the full sample.

Among the neighborhood demographics only the percent of the nonwhite population (measured at the block level) is capitalized into house prices with a negative and statistically significant effect. The estimated coefficients indicate that an increase of 1 percentage point in the proportion of the nonwhite population decreases house prices by about 22 (in the linear model) to 27 (in the quadratic model) basis points. The property tax rate does not have a statistically significant effect.

As expected, the regressions illustrate a strong relationship between school quality and house prices. The coefficient of 0.21734 in the traditional linear model (column 1) reveals that an increase in school test scores of a half SD results in a house premium of about 11 percent ($0.21734/2 = 10.867$ percent) or about \$16,000 at the mean price. A half-SD increase is equivalent to an increase of 4.6 percent in the math MAP index.

The quadratic and cubic models in columns 2 and 3 of Table 4, respectively, also indicate a large and positive linear coefficient of school quality on house prices. The coefficient for the square of the math score is, however, not statistically significant in columns 2 and 3. Interestingly, the cubic coefficient in column 3 is statistically significant, but it enters with a negative sign, which indicates that the house price premium does not monotonically increase over the range of school quality. In any case, these models suggest that nonlinearities are relevant. This is confirmed by a battery of Wald specification tests (Table 5). These tests reject the null hypothesis of a model with a constant education premium. We find that the restriction of not including a quadratic or cubic term ($\psi_2 = \psi_3 = 0$) is rejected at the 1 percent level, while not including a cubic term ($\psi_3 = 0$) is rejected at the 5 percent level. However, the restriction of no quadratic term ($\psi_2 = 0$) is not rejected. Thus, the evidence indicates that the preferred specification for the education premium in the full sample is the cubic model.

Boundary Discontinuity Models

Table 6 presents the results for the restricted boundary sample (omitting the estimated coeffi-

¹² This formula was updated in 2007 when the number of performance categories was reduced to four.

¹³ We consider the math score to be a measure of school quality superior to the reading or science measures. First, the math scores are arguably the most objective measure. Second, the distribution of the school math MAP index among the schools was contained almost entirely within 2 SDs of the mean. In contrast, the reading and science indices contained a large number of outliers, particularly in the lower tail. We did not consider the social sciences scores.

Table 5
Specification Tests: Full Sample with Neighborhood Controls

	Premium Model $f(Y) = \psi_1 Y + \psi_2 Y^2 + \psi_3 Y^3$		
	Linear	Quadratic	Cubic
Null hypothesis	$\psi_1 = 0$	$\psi_1 = \psi_2 = 0$	$\psi_1 = \psi_2 = \psi_3 = 0$
Wald F -statistic	60.757***	27.686***	30.665***
Null hypothesis		$\psi_2 = 0$	$\psi_2 = \psi_3 = 0$
Wald F -statistic		2.192	7.446***
Null hypothesis			$\psi_3 = 0$
Wald F -statistic			6.754**

NOTE: **Significant at the 5 percent level; ***significant at the 1 percent level.

coefficients for the boundary fixed effects). As in the full sample, house characteristics are statistically significant and with the expected sign. In contrast to the full sample results, the age of the building and its square, along with the square of the number of bathrooms, are statistically significant. Compared with the full sample results, the estimated coefficients for house characteristics are smaller in magnitude but very stable across specifications.

In the linear model in column 1, school quality is a statistically significant contributor to house prices and enters with the expected positive sign. Compared with the results from the full sample regression, the estimated coefficient declines in magnitude by a factor of about four. The estimate of the education premium implies that a half-SD increase (equivalent to an increase of 4.6 percent) in the average school score leads to an increase of about 3.2 percent in house prices, or about \$4,766 evaluated at the full sample mean price. This value is only slightly higher than that estimated by Black (1999). She reports a 2.1 percent increase (or \$3,948 at her sample mean) in house prices for a 5 percent increase in test scores.

The two specifications of the nonlinear boundary fixed effects models in columns 2 and 3 indicate that the quadratic coefficient of school quality is statistically significant, but the cubic coefficient is not. The positive sign of the quadratic coefficient indicates that the capitalization effect

of school quality is increasing over the range of test scores.

Specifications 1, 2, and 3 do not include additional controls for neighborhood quality other than the boundary fixed effects. As mentioned previously, some authors have raised concerns about whether the boundary discontinuity approach fails to control for omitted neighborhood characteristics and suggest that explicit additional controls be included in the estimation. We therefore include the same demographic controls as in the full sample regression—namely, the percent of female population, the percent of nonwhite population, and the percent of school-aged children, all measured at the block level. We also include the school-district property tax rate.

Columns 4, 5, and 6 in Table 6 show that these additional variables are directly capitalized into house prices. The percent of the nonwhite population is statistically significant and enters with a negative sign as in the full sample results. The magnitude of the effect is similar to the full sample results and indicates a decline of about 22 basis points in house prices for a 1-percentage-point increase in the proportion of the nonwhite population. We interpret the significance of this variable, as in other papers, as evidence of preferences about the racial composition of neighborhoods.

In contrast to the full sample results, the percent of school-aged children is statistically significant and indicates an increase in house prices of about 15 basis points for a 1-percentage-point

Table 6**Education Regressions: Restricted Boundary Sample**

Variable	Log-adjusted price					
	(1)	(2)	(3)	(4)	(5)	(6)
Math score	0.06437** (2.58)	0.06274*** (2.90)	0.04659 (1.64)	0.03227* (1.78)	0.03579* (1.93)	0.03172 (1.20)
Math score (squared)		0.02656** (2.47)	0.02909** (2.47)		0.02209** (2.48)	0.02284** (2.40)
Math score (cubed)			0.00514 (0.73)			0.00137 (0.21)
Number of bedrooms	0.03726*** (3.88)	0.03730*** (3.89)	0.03749*** (3.90)	0.03816*** (4.02)	0.03805*** (4.01)	0.03809*** (4.00)
Number of bathrooms	0.10834*** (5.78)	0.10785*** (5.80)	0.10792*** (5.82)	0.10349*** (5.81)	0.10318*** (5.82)	0.10320*** (5.83)
Number of bathrooms (squared)	-0.00529* (-1.68)	-0.00533* (-1.70)	-0.00535* (-1.71)	-0.00488 (-1.58)	-0.00491 (-1.60)	-0.00491 (-1.60)
Age of building	-0.00408*** (-2.73)	-0.00411*** (-2.75)	-0.00412*** (-2.76)	-0.00453*** (-3.11)	-0.00454*** (-3.13)	-0.00454*** (-3.14)
Age of building (squared)	0.00004*** (2.89)	0.00004*** (2.91)	0.00004*** (2.92)	0.00004*** (3.15)	0.00004*** (3.16)	0.00004*** (3.17)
Lot area (1,000s of sq. ft.)	0.00089** (2.41)	0.00089** (2.41)	0.00089** (2.41)	0.00088** (2.39)	0.00088** (2.40)	0.00088** (2.39)
Living area (1,000s of sq. ft.)	0.35315*** (15.43)	0.35228*** (15.29)	0.35236*** (15.29)	0.34332*** (15.52)	0.34297*** (15.49)	0.34301*** (15.49)
Number of stories	0.27574*** (9.30)	0.27559*** (9.30)	0.27558*** (9.31)	0.26621*** (9.55)	0.26625*** (9.57)	0.26626*** (9.57)
Number of rooms	0.05974*** (7.38)	0.05952*** (7.33)	0.05945*** (7.31)	0.05902*** (7.43)	0.05893*** (7.40)	0.05891*** (7.39)
Census block: Percent female				-0.00044 (-0.66)	-0.00039 (-0.59)	-0.00039 (-0.59)
Census block: Percent nonwhite				-0.00219*** (-3.50)	-0.00223*** (-3.56)	-0.00222*** (-3.55)
Census block: Percent people 5 to 14 years of age				0.00154** (2.25)	0.00153** (2.24)	0.00154** (2.25)
Property tax rate				-0.06787*** (-3.21)	-0.05526*** (-2.88)	-0.05465*** (-2.73)
Constant	11.13260*** (32.85)	11.12998*** (32.96)	11.13935*** (32.97)	8.86314*** (59.31)	8.72871*** (62.61)	8.72454*** (60.54)
<i>N</i>	10,190	10,190	10,190	10,182	10,182	10,182
<i>R</i> ²	0.769	0.77	0.77	0.772	0.772	0.772
Adjusted <i>R</i> ²	0.763	0.763	0.763	0.766	0.766	0.766
Boundary fixed effects	Yes	Yes	Yes	Yes	Yes	Yes

NOTE: *t*-Statistics are listed in parentheses. *Significant at the 10 percent level; **significant at the 5 percent level; ***significant at the 1 percent level.

Table 7**Specification Tests: Boundary Sample**

	Premium Model $f(Y) = \psi_1 Y + \psi_2 Y^2 + \psi_3 Y^3$		
	Linear	Quadratic	Cubic
Without neighborhood controls			
Null hypothesis	$\psi_1 = 0$	$\psi_1 = \psi_2 = 0$	$\psi_1 = \psi_2 = \psi_3 = 0$
Wald F -statistic	6.632**	4.658**	3.130**
Null hypothesis		$\psi_2 = 0$	$\psi_2 = \psi_3 = 0$
Wald F -statistic		6.115**	3.114**
Null hypothesis			$\psi_3 = 0$
Wald F -statistic			0.527
With neighborhood controls			
Null hypothesis	$\psi_1 = 0$	$\psi_1 = \psi_2 = 0$	$\psi_1 = \psi_2 = \psi_3 = 0$
Wald F -statistic	3.178*	3.581**	2.381*
Null hypothesis		$\psi_2 = 0$	$\psi_2 = \psi_3 = 0$
Wald F -statistic		6.166**	3.102**
Null hypothesis			$\psi_3 = 0$
Wald F -statistic			0.043

NOTE: **Significant at the 5 percent level; ***significant at the 1 percent level.

increase in the proportion of children between 5 and 14 years of age. The property tax rate is also statistically significant and enters with a negative sign.

The inclusion of explicit neighborhood controls does not affect the magnitude of the coefficients of the housing characteristics, but it decreases the magnitude of the linear test score coefficient by almost half. The quadratic coefficient declines only slightly. The linear coefficient on school quality remains, nevertheless, statistically significant, and the results suggest that the magnitude of the effect of school quality on house prices remains substantially large.

Wald specification tests (Table 7) confirm that, with or without the inclusion of additional neighborhood controls, the preferred specification is the quadratic model. These tests also reject, as in the full sample regressions, the null hypothesis of a model with a constant education premium. We find that the restriction of not including a quadratic or cubic term ($\psi_2 = \psi_3 = 0$) is rejected at the 5 percent level. However, the restriction of no cubic term ($\psi_3 = 0$) is not rejected.

Implicit Housing Premia

Figure 1 illustrates the preferred specification for the house pricing function with the more conservative model with boundary fixed effects resulting from the inclusion of additional neighborhood controls. The plot includes 1-SE bands.¹⁴ We argued earlier that competition in the housing market generates increasing tightness in areas associated with higher school quality, but that competition is not as prevalent in areas associated with lower school quality. The pricing function in Figure 1 confirms our argument.

The premium from school quality on housing prices is better illustrated in Figure 2. This figure is constructed from the pricing function of specification 5 in Table 6 and represents the percentage increase in house prices in response to a half-SD increase in math test scores plotted

¹⁴ The asymptotic variance of the price function was computed using the delta method as

$$\text{AsyVar}(f(\mu; \beta)) = \frac{\partial f(\mu; \beta)}{\partial \beta'} \text{AsyVar}(\beta) \left(\frac{\partial f(\mu; \beta)}{\partial \beta'} \right)'$$

Figure 1

Implied Price Function (with Neighborhood Controls)

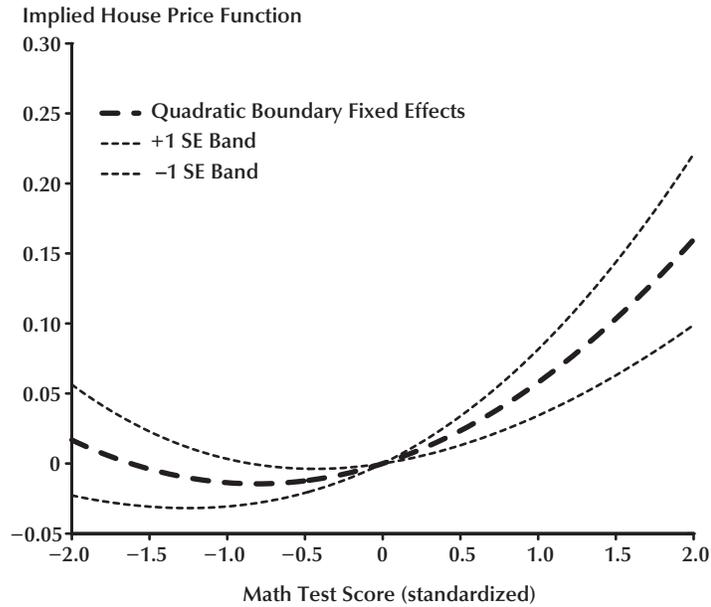
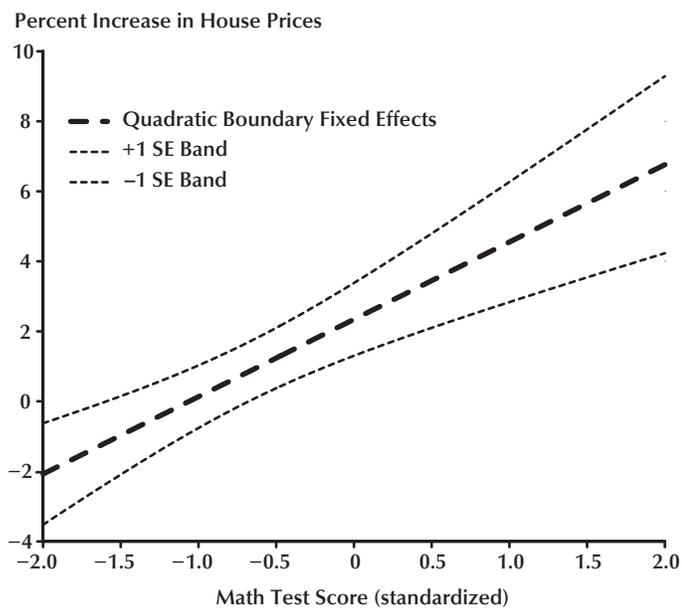


Figure 2

Implied Premium Function (with Neighborhood Controls)



NOTE: The plots show the response to a half-SD increase in math test scores.

Table 8
Implied House Price Premia from School Quality

Regression model	Full sample with neighborhood controls			Boundary sample					
				Without neighborhood controls			With neighborhood controls		
Linear coefficient	0.21734	0.22192	0.31693	0.06437	0.06274	0.04659	0.03227	0.03579	0.03172
Quadratic coefficient	—	0.03002	0.01555	—	0.02656	0.02909	—	0.02209	0.02284
Cubic coefficient	—	—	-0.03606	—	—	0.00514	—	—	0.00137
Case 1 (mean score minus 1 SD)									
Percent increase in house price	10.87	8.84	11.53	3.22	1.15	0.6	1.61	0.13	-0.01
Dollar value at mean (full sample)	16,092	13,097	17,066	4,766	1,696	885	2,389	197	-11
Dollar value at mean (boundary sample)	15,435	12,562	16,369	4,571	1,626	849	2,292	189	-10
Case 2 (mean score)									
Percent increase in house price	10.87	11.85	15.78	3.22	3.80	3.12	1.61	2.34	2.17
Dollar value at mean (full sample)	16,092	17,542	23,374	4,766	5,629	4,622	2,389	3,468	3,219
Dollar value at mean (boundary sample)	15,435	16,826	22,419	4,571	5,399	4,433	2,292	3,326	3,088
Case 3 (mean score plus 1 SD)									
Percent increase in house price	10.87	14.85	9.23	3.22	6.46	7.19	1.61	4.55	4.77
Dollar value at mean (full sample)	16,092	21,988	13,662	4,766	9,562	10,642	2,389	6,739	7,058
Dollar value at mean (boundary sample)	15,435	21,090	13,104	4,571	9,171	10,207	2,292	6,464	6,770

NOTE: The table presents the premium in house prices evaluated at different math scores resulting from a change in math score of 0.5 SD (equivalent to 4.6 percent of the mean score). The premium is computed from the logarithm specification $\Delta p/p = \Delta \ln(p) = \Delta f(\mu)$, so the percent change in house prices is given by $\Delta f(\mu) = f(\mu_1) - f(\mu_0)$ and the premium at the mean price is $\Delta f(\mu) \times \bar{p}$.

along the range of school scores within 2 SDs of the mean.

The plotted function reveals a monotonically increasing premium across the spectrum of school quality. The plot indicates that, even with the most conservative estimates, the premium for houses in areas associated with high-quality schools remains substantially large. The plot also reveals a much smaller premium for houses in areas associated with low-quality schools, where house prices seem to be driven almost entirely by housing and neighborhood characteristics other than public school quality.

Table 8 summarizes the implied school quality premia from school quality for all models and provides the dollar equivalent of the implied percentage increase in house prices relative to the mean house prices in the full and boundary samples that results from a half-SD increase in test scores.

The linear model with the full sample regression results in a constant premium of 10.87 percent or about \$16,000 at the mean house price. The cubic model in the full sample, which the specification tests suggest is the preferred model, illustrates a nonmonotonic premium that ranges from 11.53 percent for houses in areas where school quality is 1 SD below the mean to 15.78 percent in areas where school quality coincides with the average, and finally to 9.23 percent in areas where school quality is 1 SD above the mean.

The boundary sample models with and without additional neighborhood controls indicate that the premium is severely overestimated in the traditional hedonic regressions, even accounting for nonlinearities. Nevertheless, even in the most conservative estimates, the premium remains substantially large, especially for areas associated with very high-quality schools. Table 8 also shows two characteristics in the quadratic equation—the middle column of the third panel: The premium is very small in areas where test scores are 1 SD below the mean (about 0.13 percent or less than \$200) and monotonically increases in areas with higher test scores (about 2.34 percent or \$3,468 in areas with average test scores [Case 2] and 4.55 percent or \$6,739 in areas with test scores 1 SD above the mean [Case 3]).

CONCLUSION

Traditional empirical models of the capitalization of education quality on house prices have established that the quality of primary school education is positively correlated with house prices. Recent capitalization studies have used various approaches to address concerns about omitted variable bias induced by failing to account for the correlation between school quality and unobserved neighborhood characteristics. Most of these variations on the traditional hedonic approach (including the boundary discontinuity regression) have assumed that the house price premium is constant because in all these models the contribution from school quality on house prices is constrained to be linear.

In this paper, we propose an alternative formulation that allows for nonlinear effects of school quality. We show that this formulation is preferred by the data over a baseline linear boundary fixed effects model and that the rate at which the house price premium rises increases over the range of school quality. In other words, the standard linear specification for test scores overestimates the premium at low levels of school quality and underestimates the premium at high levels of school quality.

In the St. Louis metropolitan area, houses associated with a school ranked at 1 SD below the mean are essentially priced on physical characteristics only. In contrast, houses associated with higher-quality schools command a much higher price premium.

Interestingly, and in contrast to many studies in the literature, the price premium remains substantially large, especially for houses associated with above-average schools. This is true even in our most conservative estimates, which complement the boundary discontinuity approach by explicitly controlling for neighborhood demographics. These estimates also reveal that the racial composition of neighborhoods is capitalized directly into house prices.

REFERENCES

- Bayer, Patrick; Ferreira, Fernando and McMillan, Robert. "A Unified Framework for Measuring Preferences for Schools and Neighborhoods." *Journal of Political Economy*, August 2007, 115(4), pp. 588-638.
- Black, Sandra E. "Do Better Schools Matter? Parental Valuation of Elementary Education." *Quarterly Journal of Economics*, May 1999, 114(2), pp. 577-99.
- Bogart, William T. and Cromwell, Brian A. "How Much More Is a Good School District Worth?" *National Tax Journal*, June 1997, 50(2), pp. 215-32.
- Bogart, William T. and Cromwell, Brian A. "How Much Is a Neighborhood School Worth?" *Journal of Urban Economics*, March 2000, 47(2), pp. 280-305.
- Brasington, David. "Which Measures of School Quality Does the Housing Market Value?" *Journal of Real Estate Research*, 1999, 18(3), pp. 395-413.
- Brasington, David. "Edge Versus Center: Finding Common Ground in the Capitalization Debate." *Journal of Urban Economics*, November 2002, 52(3), pp. 524-41.
- Brasington, David and Haurin, Donald R. "Educational Outcomes and House Values: A Test of the Value Added Approach." *Journal of Regional Science*, May 2006, 46(2), pp. 245-68.
- Cheshire, Paul and Sheppard, Stephen. "The Welfare Economics of Land Use Planning." *Journal of Urban Economics*, September 2002, 52(2), pp. 242-69.
- Cheshire, Paul and Sheppard, Stephen. "Capitalising the Value of Free Schools: The Impact of Supply Characteristics and Uncertainty." *Economic Journal*, November 2004, 114(499), pp. F397-F424.
- Clapp, John M.; Nanda, Anupam and Ross, Stephen L. "Which School Attributes Matter? The Influence of School District Performance and Demographic Composition of Property Values." *Journal of Urban Economics*, March 2008, 63(2), pp. 451-66.
- Cushing, Brian J. "Capitalization of Interjurisdictional Fiscal Differentials: An Alternative Approach." *Journal of Urban Economics*, May 1984, 15(3), pp. 317-26.
- Davidoff, Ian and Leigh, Andrew. "How Much Do Public Schools Really Cost? Estimating the Relationship Between House Prices and School Quality." Discussion Paper No. 558, Australian National University, Centre for Economic Policy Research, July 2007.
- Downes, Thomas A. and Zabel, Jeffrey E. "The Impact of School Characteristics on House Prices: Chicago 1987-1991." *Journal of Urban Economics*, July 2002, 52(1), pp. 1-25.
- Fack, Gabrielle and Grenet, Julien. "Do Better Schools Raise Housing Prices? Evidence from Paris School Zoning." Unpublished manuscript, Paris École Normale Supérieure, October 2007.
- Figlio, David N. and Lucas, Maurice E. "What's in a Grade? School Report Cards and House Prices." *American Economic Review*, June 2004, 94(3), pp. 591-604.
- Gibbons, Stephen and Machin, Stephen. "Valuing English Primary Schools." *Journal of Urban Economics*, March 2003, 53(2), pp. 197-219.
- Gibbons, Stephen and Machin, Stephen. "Paying for Primary Schools: Admission Constraints, School Popularity, or Congestion?" *Economic Journal*, March 2006, 116(510), pp. C77-C92.
- Gibbons, Stephen and Machin, Stephen. "Valuing School Quality, Better Transport, and Lower Crime: Evidence from House Prices." *Oxford Review of Economic Policy*, Spring 2008, 24(1), pp. 99-119.
- Gill, H. Leroy. "Changes in City and Suburban House Prices During a Period of Expected School Desegregation." *Southern Economic Journal*, July 1983, 50(1), pp. 169-84.

- Hanushek, Eric A. "The Economics of Schooling: Production and Efficiency in Public Schools." *Journal of Economic Literature*, September 1986, 24(3), pp. 1141-77.
- Hanushek, Eric A. "Assessing the Effects of School Resources on Student Performance: An Update." *Educational Evaluation and Policy Analysis*, Summer 1997, 19(2), pp. 141-64.
- Haurin, Donald R. and Brasington, David. "School Quality and Real House Prices: Inter- and Intrametropolitan Effects." *Journal of Housing Economics*, December 1996, 5(4), pp. 351-68.
- Hayes, Kathy J. and Taylor, Lori L. "Neighborhood School Characteristics: What Signals Quality to Homebuyers?" Federal Reserve Bank of Dallas *Economic Review*, Fourth Quarter 1996, pp. 2-9; www.dallasfed.org/research/er/1996/er9604a.pdf.
- Hilber, Christian A.L. and Mayer, Christopher J. "Why Do Households Without Children Support Local Public Schools? Linking House Price Capitalization to School Spending." *Journal of Urban Economics*, January 2009, 65(1), pp. 74-90.
- Imbens, Guido W. and Lemieux, Thomas. "Regression Discontinuity Designs: A Guide to Practice." *Journal of Econometrics*, 2008, 142(2), pp. 615-35.
- Kain, John F. and Quigley, John M. "Evaluating the Quality of the Residential Environment." *Environment and Planning*, 1970, 2(1), pp. 23-32.
- Kane, Thomas J.; Staiger, Douglas O. and Reigg, Stephanie K. "Changing School Assignments and Housing Values." Working paper, UCLA Department of Policy Studies, 2003.
- Kane, Thomas J.; Staiger, Douglas O. and Reigg, Stephanie K. "School Quality, Neighborhoods and Housing Prices: The Impacts of School Desegregation." NBER Working Paper No. 11347, National Bureau of Economic Research, May 2005; www.nber.org/papers/w11347.pdf.
- Kane, Thomas J.; Staiger, Douglas O. and Samms, Gavin. "School Accountability Ratings and Housing Values," in William Gale and Janet Pack, eds., *Brookings-Wharton Papers on Urban Affairs*. Washington, DC: Brookings Institution, 2003, pp. 83-137.
- Leech, Dennis and Campos, Erick. "Is Comprehensive Education Really Free? A Case-Study of the Effects of Secondary School Admissions Policies on House Prices in One Local Area." *Journal of the Royal Statistical Society Series A*, 2003, 166(1), pp. 135-54.
- Oates, Wallace E. "The Effects of Property Taxes and Local Public Spending on Property Values: An Empirical Study of Tax Capitalization and the Tiebout Hypothesis." *Journal of Political Economy*, November/December 1969, 77(6), pp. 957-71.
- Reback, Randall. "House Prices and the Provision of Local Public Services: Capitalization Under School Choice Programs." *Journal of Urban Economics*, March 2005, 57(2), pp. 275-301.
- Ridker, Ronald G. and Henning, John A. "The Determinants of Residential Property Values with Special Reference to Air Pollution." *Review of Economics and Statistics*, May 1967, 49(2), pp. 246-57.
- Rosen, Sherwin. "Hedonic Prices and Implicit Markets: Product Differentiation in Pure Competition." *Journal of Political Economy*, January/February 1974, 82(1), pp. 34-55.
- Rosenthal, Leslie. "The Value of Secondary School Quality." *Oxford Bulletin of Economics and Statistics*, July 2003, 65(3), pp. 329-55.
- Ross, Stephen and Yinger, John. "Sorting and Voting: A Review of the Literature on Urban Public Finance," in Paul Cheshire and Edwin Mills, eds., *Handbook of Regional and Urban Economics. Volume 3: Applied Urban Economics*. Chap. 47. Amsterdam: North Holland, 1999, pp. 2003-060.

Chiodo, Hernández-Murillo, Owyang

Sheppard, Stephen. "Hedonic Analysis of Housing Markets," in Paul Cheshire and Edwin Mills, eds., *Handbook of Regional and Urban Economics. Volume 3: Applied Urban Economics*. Chap. 41. Amsterdam: North Holland, 1999, pp. 1595-635.

Thorsnes, Paul and Reifel, John W. "Tiebout Dynamics: Neighborhood Response to a Central-City/Suburban House-Price Differential." *Journal of Regional Science*, October 2007, 47(4), pp. 693-719.

Tiebout, Charles M. "A Pure Theory of Local Expenditures." *Journal of Political Economy*, October 1956, 64(5), pp. 416-24.

Weimer, David L. and Wolkoff, Michael J. "School Performance and Housing Values: Using Non-Contiguous District and Incorporation Boundaries to Identify School Effects." *National Tax Journal*, June 2001, 54(2), pp. 231-53.

Wheaton, William C. "Vacancy, Search, and Prices in a Housing Market Matching Model." *Journal of Political Economy*, December 1990, 98(6), pp. 1270-92.

Williams, Joseph T. "Pricing Real Assets with Costly Search." *Review of Financial Studies*, Spring 1995, 8(1), pp. 55-90.