Money Stock Control and Its Implications for Monetary Policy*

by ALBERT E. BURGER, LIONEL KALISH III, and CHRISTOPHER T. BABB

In the last two years there has been an increased concern within the Federal Reserve System about the role of monetary aggregates in policy, and about the operating procedures implicit in the policy directive of the Federal Open Market Committee. A collection of studies on these subjects, Open Market Policies and Operating Procedures - Staff Studies, was published by the Board of Governors in 1971. Other economists have presented methods for analyzing the effects of different growth rates of money on policy objectives. An equally important subject is the controllability of different aggregates and the effect this controllability would have on the ability of policymakers to achieve policy objectives.

This article presents a procedure that could be used by the Federal Reserve System to control the growth of the money stock and a method for evaluating the effect of this control procedure on the ability of policymakers to achieve their policy objectives.

A growing volume of research has demonstrated that changes in the money stock are a reliable summary measure of the effect of monetary policy actions on economic activity. One result of this research has been the suggestion that the monetary authorities could best achieve ultimate policy objectives, such as full employment and stable prices, by controlling the growth rate of the money stock. Such a suggestion requires (1) an operational procedure for controlling money, and (2) a means of assessing the implications of such a procedure for the ability of policymakers to achieve their policy objectives.

A possible procedure for monetary policy includes:

1. The Federal Open Market Committee (FOMC) decides upon the ultimate objectives of monetary policy, such as desired growth rates for real output and prices, and a desired level of employment.

2. These ultimate objectives are related to a growth rate of money, and the FOMC issues a "directive" to the Trading Desk to obtain this growth rate for money.

3. The Trading Desk uses open market operations to achieve the growth rate of money which is consistent with the policymaker's objectives.

This article is concerned with the actual implementation of policy decisions. It is not concerned with how the policymakers decide upon their ultimate objectives, or with the specific way in which these objectives are related to a growth rate for money. The policy objectives are taken as given. Converting policy objectives into a desired growth rate of money requires information on the linkage between changes in the growth rate of the money stock and the ultimate objectives. Such information can be derived from competing models of income or spending determination.

This article presents a procedure the Federal Reserve could use to control money and a method for evaluating the effect of this control on the policymakers' ability to achieve GNP objectives. The money stock control procedure requires only that the Federal Reserve has information about the previous three

*The authors wish to express their thanks to the many people who read earlier drafts of this article. A special obligation is due the following economists who, in working sessions or otherwise, offered specific comments: Professors Milton Friedman, Arnold Zellner, Robert Gordon, Richard Zeckhauser, Stanley Fischer, Allan Meltzer, Michele Fratianni, William Yohe, David Fand, and Messrs. Paul Meek and Wolfgang Gebauer. As always, we benefited from comments and criticism of the research staff at the Federal Reserve Bank of St. Louis. The procedures and conclusions are the responsibility of the authors and do not necessarily reflect the views of any of the commentators on the article or the Federal Reserve System.

The FOMC issues a policy directive to the New York Federal Reserve Bank. The Trading Desk at the New York Bank carries out day-to-day open market transactions (purchase and sale of Government securities) for the System. The text of each policy directive issued by the FOMC is made public about 80 days after each FOMC meeting and published in the Federal Reserve Bulletin.
Money Stock Control Procedure

There are two major ways in which the Federal Reserve might operate to control the growth of money. One way is to estimate the money market conditions that would be consistent with the growth rate of money stated in the directive, and then operate to achieve these conditions in the money market. This approach might involve choosing bounds for the Federal funds rate and free reserves and then operating on a day-to-day basis to maintain money market conditions within these bounds. A second method of money stock control, the one discussed in this article, involves estimating the changes in the source base (or some other reserve aggregate) required to achieve the policy determined growth path for money. The Federal Reserve would then operate on a day-to-day basis to determine the growth of the source base.2

The money stock control procedure used in this article is developed from a multiplier-base framework, within which the money stock \( (M) \) is expressed as:

\[
M = mB.
\]

In this expression \( B \) denotes the net source base and \( m \) represents the money multiplier. An increase in Federal Reserve holdings of securities, float, the gold stock, and Treasury currency outstanding will increase the net source base. An increase in Treasury deposits at the Federal Reserve, Treasury cash holdings, and other deposits and other Federal Reserve accounts will decrease the net source base. A complete listing of the sources and uses of base money and the relationships between the net source base, source base, and monetary base are given in Table I.

The net source base is taken as the control variable for the process.4 From the sources side, the major component of the net source base (about 75 per cent) is Federal Reserve holdings of Government securities. The Federal Reserve is assumed to be able to accurately measure and determine the magnitude of the base within a monthly period. Evidence on the accuracy with which the Federal Reserve has been able to forecast and measure the net source base is presented in the working paper of technical appendices.5

The money multiplier \( (m) \) summarizes all other factors involved in the money supply process. The money multiplier responds to portfolio decisions by the commercial banks, the Treasury, and the public. Also included in this formulation of the multiplier are the influences of reserve requirement changes, the discount rate, and Regulation Q.6

In our money stock control procedure the Federal Reserve decides upon the desired growth rate of

\[m = \frac{1 + k}{r - (b + t + d) + k}\]

where \( k \) and \( d \), respectively, are the ratios of currency held by the public and U.S. Government deposits at commercial banks to the demand deposit component of the money stock.

\( r, b, \) and \( t, \) respectively, are the ratios of bank reserves, member bank borrowings, and time deposits to commercial bank deposit liabilities (excluding interbank deposits).

The reserve ratio (through the dependence of banks’ desired excess reserves), the borrowing ratio and the time deposit ratio are all dependent upon credit market interest rates.


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2These two methods of money stock control are not independent of each other. Open market actions taken to determine money market conditions will influence the growth of the base, and actions taken to influence the base will affect short-term money market conditions. See, Albert E. Burger, "The Implementation Problem of Monetary Policy," this Review (March 1971).

3The data requirements for controlling the net source base are as small or smaller than any of the other major aggregates commonly suggested as operating targets for the Federal Reserve. Richard Davis has shown that out of a wide range of possible aggregate targets the nonborrowed base and nonborrowed reserves would be the easiest targets for the Desk to hit. These two targets are entirely exogenous with respect to open market operations. Contrary to other proposed targets, success in hitting these two targets does not depend upon the Desk offsetting items whose movements are functionally related to open market operations. See Richard G. Davis, "Short-Run Targets for Open Market Operations," Open Market Policies and Operating Procedures-Staff Studies, Board of Governors of the Federal Reserve System, July 1971, pp. 37-70.


5The money multiplier associated with the net source base is:

\[
m = \frac{1 + k}{r - (b + t + d) + k}
\]

where \( k \) and \( d \), respectively, are the ratios of currency held by the public and U.S. Government deposits at commercial banks to the demand deposit component of the money stock.
money, converts this growth rate into desired money stock levels for the control periods, and forecasts the money multiplier (m) for the control periods. Then during the control periods, the Federal Reserve uses open market operations to attain the net source base (B) such that the product (mB) equals the desired money stock levels. Implementing mnonetary policy under such a money stock control procedure requires three considerations: (1) the length of the control period; (2) a procedure for forecasting the money multiplier; and (3) the response to previous errors in money stock control.

**Control Period**

The maximum acceptable time period for forecasts of the multiplier depends upon the relationship between changes in money and changes in economic activity. Empirical evidence indicates that quarter-to-quarter changes in the growth rate of money influence economic activity. Therefore, the maximum time period over which the Federal Reserve would aim to control the money stock would be a quarterly period. Such an assumption, however, leaves open the possibility of sharp fluctuations in the growth of money over the quarter. Therefore, it is further assumed that as an operating strategy, it is preferable to minimize the expected squared deviation of the monthly value of money from its desired growth path. The net source base is assumed to be controllable on a daily-average monthly basis; therefore, within our control procedure monthly average multipliers are forecast. Having predicted the value for the month's money multiplier, and given the desired level for the money stock in that month, the average monthly value for the net source base necessary to achieve the desired growth of money is determined.

**Forecasting the Money Multiplier**

Next period's multiplier might be forecast by any one of the following methods:

1. **Definitional method** — The multiplier-base framework is treated as an accounting identity. Some of the ratios of the multiplier are forecast using information about the various components (for example, Treasury deposits) acquired by the Desk in its daily operations. Other elements of the ratios are treated as being equal to their previous values with some adjustment for trend or seasonal variation.

2. **Regression method** — The money multiplier is expressed as a function of variables that are known or are under the policy control of the Federal Reserve at the time each forecast is made. This relationship is estimated each period by multiple regression analysis.

3. **Behavioral method** — Each of the ratios of the multiplier is expressed as being dependent upon other variables such as interest rates, policy instruments, and other factors influencing the deposit behavior of the banks and the public. This procedure requires predicting these other variables.

In this article, the second method is used. Each month's multiplier is forecast using the three-month moving average of past values of the multiplier, reserve adjustment magnitude in the forecast month,
dummy variables to account for seasonal factors, and an adjustment for autocorrelation. The values of these independent variables are known to the Federal Reserve.\(^8\)

**Response to Previous Errors in Money Stock Control**

If there are errors in the forecasts of the money multiplier, the desired growth of money and the controlled growth of money will not be the same in every period. Under these conditions, further information is required to determine the optimal setting for the net source base. Suppose in period \(t_1\) the money managers over-predict the money multiplier. Consequently, the achieved growth of money is less than the desired growth rate. What is the optimal setting for the net source base in period \(t_2\)? Should the money managers ignore the shortfall of money in \(t_1\)? Should they try and make up the shortfall of money in \(t_1\) by setting the net source base in \(t_2\) so that the growth of money is above the desired growth path? If they try and make up all of the gap in \(t_2\), or only part of the gap in \(t_2\) and the remainder in succeeding periods?\(^9\)

There are many possible error-response mechanisms. Our procedure assumes that the money managers assign proportionally more weight to large errors in money stock control than small errors. Therefore, the error-response mechanism is designed to minimize the expected value of the squared deviations of controlled money from its policy chosen growth path.\(^9\) At the end of each control period, the money managers compute their error in money stock control. During the next control period the net source base is set approximately to make up last period’s error.\(^10\)

The money stock control procedure is illustrated in the following exhibit.

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\(^8\) The Federal Reserve sets member bank reserve requirements. Since, under the current lagged reserve requirement procedure the effect on member bank required reserves of a change in reserve requirements effective this week depends upon member bank deposits subject to reserve requirements two weeks earlier, the Federal Reserve can accurately determine the effect of a change in reserve requirements on the reserve adjustment magnitude.

\(^9\) This error-response mechanism assumes a quadratic loss function for the money managers. The control periods’ base values are determined by minimizing the expected value of the loss function with respect to \(B\). For a discussion of this procedure see the Appendix at the end of this article.

\(^10\) If only the growth rate of money mattered, then the money managers would not attempt to make up last period’s error in the level of money. Each period the money managers would try to move along the desired growth path from where they were last period.

**Simulation of Money Stock Control and GNP**

How would the money stock control achieved by this procedure affect the ability of the Federal Reserve to achieve policy objectives? To gain some information on this question, the money stock control procedure was simulated over two sample periods,
and the effects of these simulation results on GNP were analyzed. First, the method and results of simulating the money stock control procedure are presented. Then, the method of relating changes in money to GNP is discussed, and the results of simulating GNP when money is controlled without error are compared to the case where money is controlled by our procedure.

Simulation of the Money Stock Control Procedure

The following method was used to simulate money stock control:

1. It was assumed that the policymakers choose a constant 4 per cent seasonally adjusted annual growth rate for money over the control period.11

2. The Federal Reserve adjusts the net source base in the current month to minimize the expected value of the squared deviation of the achieved monthly stock level from the original 4 per cent growth line.12

3. Two control periods were chosen, 1962 through 1965 and 1966 through 1969. The base periods were chosen as fourth quarter 1961 and fourth quarter 1965.

4. Each month, the money stock achieved by the control process (controlled money) is computed by taking the level of the net source base determined by our operating strategy and multiplying it by the value of the multiplier that actually prevailed in that month.13 To the extent that the forecast multiplier is different from the one that actually prevailed in that month, the achieved level of money is different from the desired.

The example in Table II, which may be used to illustrate this procedure, should be taken only as an illustration. For the technical aspects of the procedure, especially the error-response mechanism, consult the Appendix at the end of this article. The first column in Table II gives the monthly money stock levels consistent with the growth rate of money that the policymakers are advised will give them their desired policy objectives. The second column gives the forecast of the multiplier and the fifth column gives the money multiplier that actually prevailed in each month. It is assumed that the control procedure begins in January. For the first two months the Federal Reserve forecasts the multiplier with complete accuracy, the net source base is changed by $4 billion, and the money stock achieved by the control procedure equals the desired.

In March, however, there is an error in the forecast of the multiplier. The multiplier is forecast to be 2.51, when it actually (the historical value) is 2.50. Consequently, the net source base is increased by only $0.8 billion. Based on a forecast of 2.51 for the multiplier, the Federal Reserve expects that it would only have to supply $0.8 billion of base, compared to $4.0 billion in the previous two months. The result is an error in money stock control, controlled money is less than desired ($202.2 billion compared with a desired level of $203 billion). In April, the Federal Reserve again forecasts the multiplier correctly. In this month the net source base is increased enough to make up last month's money stock error, and to hit the target of $204 billion.14

The desired growth rate of money was converted into desired monthly levels in the following manner: (1) the averages of money in IV/61 and IV/65 were taken as the base period; (2) these base values were placed on December of 1961 and December 1965; (3) to compute the conversion factor for a 4 per cent growth rate we divided .04 by 12 to yield .00333; and (4) each month's desired money stock level was equal to (base month) + (base month) x (number of months out from base month) x (.00333). For example, December 1966 desired level equals (167.0099) + (167.0099) (12) (.00333) = $173.75 billion, where 167.0099 equals the average of the last three months of 1965.

This procedure yields a simple 4 per cent growth rate of money that appears as a straight line on an arithmetic scale. When computing quarter-to-quarter growth rates of money, however, the desired rate will be below 4 per cent near the end of the period. The results of our procedure would not have been altered if we had used a compounded annual rate for money.

11 This procedure assumes the independence of changes in the net source base and the multiplier. If m and B are not independent, then the actual multiplier might not be the one that prevailed, given a different change in B. For a discussion of this condition see Lionel Kalib, "A Study of Money Stock Control," Journal of Finance (September 1970), pp. 761-776.

12 This example uses an absolute loss function. To minimize the expected value of the squared deviations of money, the
There are two prevalent views among economists concerning the constancy of the desired rate of change of the money stock.\textsuperscript{15} One view is that the desired rate of change should never be altered (seasonally or cyclically). An alternative view holds that the monetary authorities have enough knowledge to alter the monetary growth rate seasonally and cyclically so that economic goals can be achieved better than if the rate were held constant. This particular issue does not affect our control procedure. The choice of a constant 4 per cent growth rate for money does not necessarily imply that a 4 per cent rate was a desirable monetary growth path for this period. Different desired rates of change mean only that the monetary authorities aim for different money stock levels, and combined with the same forecasted multiplier, the only difference in the operating strategy would be a different change in the net source base.

Comparison of the sample periods — In order to gain information about the stability and robustness of the money stock control procedure, it was simulated during two historical periods which were markedly different with respect to the stability of the money multiplier. A change in any of the ratios appearing in the money multiplier (see footnote 6) can alter the value of the multiplier. These ratios are influenced by a number of factors such as market interest rates, the relationship between Regulation Q ceiling rates and market rates, Treasury deposit decisions and changing patterns of tax payment dates, and introduction of changes in reserve requirements such as lagged requirements in September of 1968.

Therefore, in periods where there are sharp or erratic changes in the factors influencing the multiplier, one might expect the errors in predicting the multiplier to be larger than in periods where these factors remain constant or follow a steady trend.\textsuperscript{16} The following chart shows the variation of the money multiplier about its trend during both sample periods. Comparing the behavior of the historical money multiplier, it can be seen that it exhibited much greater variability in the 1966-69 sample period than in the 1962-65 period.

Empirical results — The results of simulating money stock control over the two sample periods are illustrated in the following chart.\textsuperscript{17} Table III presents several alternative ways of evaluating the results of our control procedure. This table presents controlled and desired levels, controlled and desired growth rates, and includes the mean, variance, mean square, and median of the errors.

Although the underlying conditions for money stock control are quite different in the two sample periods, the mean value of differences between controlled and desired growth rates is approximately the same in both periods. The mean value of deviations of controlled and desired levels is somewhat larger in the 1966-69 period. However, relative to the levels involved, the average percentage errors these deviations represent is approximately the same for the 1966-69 period as for the 1962-65 period.

The major difference between the results of the control procedure in the two periods is the occurrence of somewhat more frequent large deviations in the 1966-69 period. One indication of this difference is that the mean squared error for differences in the levels for the latter sample period is 8.62 billion, compared to 3.36 billion in the earlier period. Also, the average for the five largest percentage errors in the levels is 0.65 per cent in the latter period, compared to 0.58 per cent in the earlier period.

Projections of GNP

Policymakers are primarily concerned with attaining ultimate policy objectives, not just with controlling the growth of money. Controlling money is a means to an end, not the end in itself. In this section, the growth of GNP implied by a constant 4 per cent growth rate of money is chosen as the policy objective. This policy objective path for GNP (desired GNP) is then compared to the growth of GNP at


\textsuperscript{16}The three interest rate series, commercial paper rates, market yields on Treasury bills, and long-term corporate bond rates, all exhibited much greater variation in the 1966-69 period. Examination of the t, k, and r-ratios also reveals a pattern of increased variability and sharp erratic movements in these ratios in the latter period. Of special interest is the behavior of the t-ratio (time deposits/demand deposits of money) in the two periods. In the 1962-65 period the t-ratio follows a steady upward trend with only a small amount of variation about the trend. In contrast, the t-ratio during the 1966-69 period exhibits wide and erratic fluctuations about its trend line. In the 1966-69 period the contribution of the t-ratio to the month-to-month percentage change in the historical money stock had a mean of —57 per cent and a variance of 4.48, compared to a mean of —2.23 per cent and a variance of .76 in the 1962-65 period. There are pronounced changes in the pattern of the t-ratio in the last half of 1966, in 1968, and during 1969. These changes reflect primarily the constraint of Regulation Q, which was an additional factor influencing the money supply process in the latter period.

\textsuperscript{17}Charts plotting monthly values of controlled money are given in Working Paper No. 14.

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A model linking changes in the money stock to changes in nominal GNP was chosen. The model used was the Andersen-Jordan (A-J) spending equation which relates changes in GNP to current and lagged changes in the money stock and high employment government expenditures.\(^\text{19}\)


1 Actual high-employment government expenditures were used in both simulations. This procedure assumes that forecast high-employment government expenditures are always equal to the actual.

3 The A-J equation was used to project quarterly GNP with a constant 4 per cent growth of money. This projected GNP path is the policy objective. Then, the A-J equation was used to project GNP for the same period, with the growth pattern of money as generated by our control procedure when aiming at a constant 4 per cent money stock growth. This is the GNP...
that would have actually resulted from policy actions. ¹⁵

Several important points about this procedure should be emphasized. It is assumed that the GNP

that would have resulted from a constant 4 per cent growth rate of money and from controlled money would have been the GNP projected by the equation relating changes in money to changes in GNP. Therefore, the only source of error between the policy objective GNP and the GNP resulting from money stock control is the error in money stock control.

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Second, instead of the A-J equation, any other econometric model that relates changes in money to changes in nominal GNP could have been used. Other economists might work out the implications of this and other money control procedures for the ability of policymakers to hit a desired value of GNP, using alternative forecasting and structural models of the economy. Such results would provide valuable supplemental evidence on the adequacy of proposed money stock control procedures.

A third point is that only the influence of money stock control on nominal GNP was considered. The ultimate objectives of monetary policy are variables such as employment and prices. However, this article is not concerned with the influence of different GNP growth rates on employment and prices. It is assumed that the policymakers pick desired values for employment and prices and then convert these into a desired growth rate of nominal GNP. An analysis of what a given growth of GNP implies for prices and employment could be carried out by using a larger model.

**Empirical results** — The results of the GNP simulations are presented in Table IV and the following chart. The monetary policymakers are assumed to have chosen objectives for GNP, and then, based on the information they have about the relationship between money and GNP, they have decided that a 4 per cent monetary growth rate will best achieve these GNP objectives. The second column of Table IV contains the growth path of GNP the policymakers desire to achieve (quarterly averages of nominal GNP projected by the A-J equation when a constant 4 per cent growth rate of money is assumed). The first column of this table shows the quarterly averages of nominal GNP projected by the A-J equation when the money stock resulting from our operating procedure for those years is read into the A-J equation.

At an operational level, the Trading Desk is directed to follow an open market policy to achieve the 4 per cent growth rate of money. To carry out its “directive,” the Trading Desk forecasts the money multiplier by our procedure, and then supplies the amount of net source base each month that is required to achieve the level of the money stock consistent with the 4 per cent growth of money. Since there are deviations between the quarter-to-quarter growth rate of money achieved by the control procedure and the desired 4 per cent rate, there are deviations of achieved GNP from the policy objective.

Under the simulation exercise, the success of the policymakers in achieving their desired GNP objectives on average is approximately the same in both sample periods. The largest percentage error in the levels is seven-tenths of one per cent, and in both periods 10 of the 16 quarterly misses are three-tenths of one per cent or less. The mean difference between money stock control and policy objective (desired) quarter-to-quarter growth rates of GNP is .01 per cent in the 1962-65 period and .02 per cent in the 1966-69 period.

The simulations indicate that the Federal Reserve would have been about equally successful in achieving its GNP objectives in both periods. This result follows from two conditions. First, although there are more frequent large deviations in the achieved money stock in the 1966-69 period, they are not maintained for a long period. On average the degree of control is about the same in both sample periods; deviations
above the desired growth path are followed by deviations below the growth path. Second, in the GNP equation, the influence of changes in the growth rate of money are distributed over time. The whole impact of a change in money on GNP does not occur in the same quarter. The influence of money on income includes the growth of money over the preceding four quarters.

Assessing the Effect of Money Stock Control on Policy Objectives

In the previous section, the growth path of GNP projected assuming no errors in money stock control was compared to GNP projected with money stock control using our control procedure. The comparisons were made for two sample periods. However, even
### Table IV

#### Nominal GNP Levels and Compounded Annual Rates of Change

Generated by the Andersen-Jordan Equation

#### (Billions of Dollars)

1962-1965

<table>
<thead>
<tr>
<th>Quarter</th>
<th>Controlled Level</th>
<th>Desired Level</th>
<th>Difference Between Controlled and Desired Levels</th>
<th>Per Cent Error Between Controlled and Desired Levels</th>
<th>Difference in Annual Quarter-to-Quarter Growth Rates</th>
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<td>1962 I</td>
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<td>-.5%</td>
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<tr>
<td>II</td>
<td>553.54</td>
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<td>-4</td>
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<tr>
<td>III</td>
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<tr>
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</table>

Mean of deviations: Absolute 1.89
Mean of deviations: With Sign 1.88

Mean of Per Cent Error: Absolute .32
Mean of Per Cent Error: With Sign .32

Mean of Difference in Growth Rates: .01

### 1966-1969

<table>
<thead>
<tr>
<th>Quarter</th>
<th>Controlled Level</th>
<th>Desired Level</th>
<th>Difference Between Controlled and Desired Levels</th>
<th>Per Cent Error Between Controlled and Desired Levels</th>
<th>Difference in Annual Quarter-to-Quarter Growth Rates</th>
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<td>III</td>
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<td>.2</td>
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<td>817.67</td>
<td>-1.20</td>
<td>-1.1</td>
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<td>829.78</td>
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<td>.1</td>
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<tr>
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<td>.21</td>
<td>.0</td>
<td>-.1</td>
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</table>

Mean of deviations: Absolute 2.32
Mean of deviations: With Sign 1.90

Mean of Per Cent Error: Absolute .29
Mean of Per Cent Error: With Sign .43

Mean of Difference in Growth Rates: .02

### Footnotes

1Assuming a simple 4 per cent growth rate for money.
2Compounded annual rates.
though the control procedure worked reasonably well during the sample periods, it will not necessarily do as well in some time interval outside the sample periods.\footnote{This result can occur because the point estimates of the parameters of the model differ from their unobservable population values.}

In an actual policy application, the procedure would be used outside the sample period. Therefore, policymakers must have some means of assessing what a suggested control procedure implies for their ability to achieve policy objectives in a forecasting situation. This criterion can be a comparison of the ability to attain policy objectives when there are no errors in the control procedure, with the case where there are errors in the control procedure. In this article GNP was chosen as the policy objective, and policy was implemented using a money stock control procedure. Therefore, the basis for judging the control procedure is the amount by which the errors in money stock control add to errors in forecasting the GNP that would result from a desired growth rate of money.

In this section, representative GNP prediction confidence intervals are presented. In arriving at these confidence intervals, allowance is made for the reliability of the sample estimates of the model's parameters and the multiplier forecasts. A modified standard error of forecast statistic is used to specify confidence intervals for GNP projections when money is controlled. These confidence intervals are then compared with confidence intervals for GNP projections when there are no errors in money stock control.\footnote{The deviation of the SEF statistic and the technical aspects of specifying these confidence intervals are discussed in the Appendix at the end of this article, and in the technical appendices available in Working Paper No. 14.}

Table V presents 95 per cent confidence intervals for GNP projections, assuming no errors in money stock control for the four quarters of 1970. The final column in Table V presents the probability of the actual value of GNP falling within these same confidence intervals, given that our control procedure is used to control money. For example, there would have been a 95 per cent probability of actual GNP being within ±$8.64 billion of the projected level in II, 1970, assuming there was no possibility of errors in money stock control. If money had been controlled by our procedure, there would have been a 93.94 per cent probability of actual GNP being within ±$8.64 billion of the projected level. On average, over the four quarters in 1970, money stock control would have reduced the probability of the actual value of GNP falling within the given confidence interval from 95 per cent to 93.3 per cent. These results indicate that, for 95 per cent confidence intervals, the errors in money stock control implied by our control procedure would have had only a very small effect on the policymaker's ability to forecast GNP.

### Conclusions

The implementation procedure for monetary policy developed in this article provides the basis for a well-defined operational procedure for controlling money. The money stock control procedure does not require the use of any information which the Federal Reserve does not already have available. In fact, it greatly simplifies the operating instructions which would be issued to the Trading Desk. The FOMC would issue a directive to the Trading Desk stating in terms of a growth rate for money. The Desk would convert this growth rate of money into a monthly daily-average net source base figure by using the procedure developed in this article to forecast the monthly money multiplier. During each month, the Desk would use open market operations to set the net source base at the level consistent with the growth rate of money stated in the directive. The Desk would not have to interpret the "consensus of the members of the FOMC." Each month the Desk would have a precise monthly daily-average net source base figure to attain.

Using a simulation technique, this article presented evidence on the effect this money stock control pro-
procedure would have had on the ability of policymakers to achieve GNP objectives. In both of the four-year sample periods the largest percentage error in GNP levels was less than one per cent, and in each period 10 of the 16 quarterly GNP errors were three-tenths of one per cent or less. To assess the effect of money stock control, moving outside the sample periods, the standard error of forecast statistic was developed to permit the construction of appropriate confidence intervals for GNP projections. For the four quarters of 1970, the money stock control procedure only reduced the probability associated with the 95 per cent confidence interval to 93.3 per cent.

The final judgement on any monetary policy procedure ultimately rests with the members of the Federal Open Market Committee. As an ideal situation the FOMC would want no errors in achieving their policy objectives. However, this ideal cannot be realized. Therefore, the policymakers must have some means of comparing the effects of different control procedures on their ability to achieve their policy objectives. This article presented some information on these matters for a money stock control procedure.

The Federal Reserve in operating such a money stock control procedure would have additional information that could be used to more closely monitor its control process. The multiplier-base framework used in this article is taken from a fully developed specification of the money supply process, within which the influence of changing economic conditions on the money supply process may be analyzed. Also, a percentage change in the money stock may be decomposed into the percentage changes due to the net source base and the multiplier. The percentage change in the multiplier may then be broken down into the percentage change due to each of its components. For example, at times when large inflows and outflows of time deposits are induced by changes in market rates relative to Regulation Q ceilings, this factor may exert an important influence on the money multiplier. Using this additional information, the Federal Reserve should be able to improve its control of the money stock.22

When a money stock control procedure is suggested, a question that is frequently raised is "What does such a procedure imply for the stability of the money market?" The Federal funds rate is commonly used as a summary measure of short-run (daily or weekly) conditions in the money market. If, as implied in our simulations, the Desk had exactly achieved its targeted net source base level each month, would there have been significantly greater fluctuations in the Federal funds rate? The answer to this question required the use of a tested, very short-term, money market model that relates daily or weekly fluctuations in the Federal funds rate to changes in the net source base. Unfortunately, such a model is not available. Using quarterly models, some evidence can be gained on the quarterly average results of money stock control on interest rates. However, these results are not satisfactory to individuals interested in daily or weekly fluctuations.

The money stock control procedure in this article does not necessarily require that the Desk hit the targeted level for the net source base each day or week of the month. The Desk is to attain a daily-average monthly net source base target. Therefore, as a practical operating strategy, the Desk would have some latitude to offset short-term shocks to the money market within each month. However, the Desk would have to give primary consideration to achieving the net source base target. The Desk would have to guard against allowing one short-term special situation to be followed by another, resulting in a deviation of the target base level from the one necessary to achieve the desired monetary growth path.

One tentative piece of evidence related to the problem of aggregate control versus money market stability has been presented by Richard Davis.23 Davis analyzed the effect that control of nonborrowed reserves would have had on short-term money market rates for a sample period in 1967. He concluded that

Having said that certain features of the experiment tend to overstate the degree of potential money market instability, however, the writer is inclined to the view that the degree of instability indicated is nevertheless rather surprisingly mild. The computed-average absolute weekly change in the Federal funds rate tends to be only around 50 basis points, certainly substantially larger than the average changes

22Also, this procedure does not imply that the value of the multiplier forecast for the coming month at the end of this month should be the one used throughout the month. Each week of the month, as new data on the money stock in the preceding period becomes available, a new forecast of the monthly multiplier could be prepared. Based on this additional information, the net source base target for the month might be altered.
that actually occurred (around 17 basis points), but not more than the market would seem able to handle without undue stress.\textsuperscript{24}

It is important to the well-being of the whole economy that monetary policy be implemented using the procedure that offers the highest probability of policymakers achieving their policy objectives. Other economists have proposed alternative strategies for implementing policy. However, a useful comparison of our procedure with these alternative procedures can only take place when these alternatives are explicitly formulated and the effects on GNP of using these procedures is illustrated. Criticism of this money stock control procedure is welcomed. Proponents of other policy procedures are challenged to explicitly formulate their proposals so the effects of these procedures on attaining policy objectives can be analyzed. In this manner monetary policy can be implemented and improved on the basis of empirical evidence, rather than implemented on the basis of conjecture, personal belief, and tradition.

\textbf{APPENDIX}

In this appendix the technical aspects of the forecasting equation for the money multiplier, the error response mechanism, and the development of the standard error of forecast statistic are presented.

\textbf{Forecasting Equation for the Money Multiplier}

Each month's multiplier is forecast using the following equation:\textsuperscript{25}

\[ \hat{m}_t = b_0 + b_1 X_{1t} + b_2 X_{2t} + \sum_{i=1}^{11} b_{i+2} d_i + \rho \mu_{t-1} \]

where: (1) \( X_1 \) = three month moving average of past value of the multiplier,

\( X_2 \) = reserve adjustment magnitude in the forecast month,

\( d_i \) = dummy variables to account for seasonal factors,\textsuperscript{26}

\( \rho \) = the correlation coefficient for consecutive error terms in the equation during the sample period,

\( \mu_{t-1} \) = lagged value of the error in the estimate of the money multiplier.

(2) The coefficients \( b_i \) are estimated by least squares using the previous 36 months' observations. Each month the coefficients are re-estimated by adding the most recent month and dropping the first month of the previous 36 observations. \( b_0 \) is an intercept term which also acts as a seasonal dummy variable. The influence of the \( d_i \) is to shift the intercept from period to period.

(3) The reserve adjustment magnitude is introduced to capture the effects of reserve requirement changes. Reserve adjustments are expressed in dollar amounts which are positive when average reserve requirements fall and are negative when reserve requirements rise.\textsuperscript{27}

(4) The regression equation's Durbin-Watson (D-W) statistic indicates the existence of significant autocorrelation in the equation's errors. With this condition it is possible to get improved estimates of the money multiplier over time by including an additional variable in the prediction equation. This variable which "allows" for the autocorrelation is the lagged value of the error (\( \mu_{t-1} \)) in the estimate of the money multiplier times the correlation coefficient \( \rho \) for consecutive-error terms in the equation during the sample period.\textsuperscript{28}

One means of judging the forecasting ability of the multiplier equation is to compare the root mean square

\textsuperscript{24}Davis, p. 61.

\textsuperscript{25}Parameter estimates of the monthly forecasting equations are included in the technical appendices in Working Paper No. 14.

\textsuperscript{26}Similar results were obtained by omitting the seasonal dummy variables and instead adjusting not seasonally adjusted money by the seasonal factors used by the Federal Reserve.

\textsuperscript{27}Shifts of deposits between banks with different legal reserve requirements and between different deposit categories also exert a slight influence on the month-to-month changes in the reserve magnitude. The variance of the monthly first differences of the reserve adjustment magnitude during 1963-69 was six times greater when all months were included, than when months in which reserve requirement changes took place (and adjacent months) were excluded. For the 1962-69 period, except for months where reserve requirements were changed, the Federal Reserve could have assumed the forecast month's reserve adjustment magnitude would be the same as the current month's value without an appreciable error over the period.

\textsuperscript{28}This technique assumed first order autocorrelation. \( \rho \) is estimated as

\[ 1 - \frac{\text{DW}}{2} \]
error (RMSE) of the forecasting procedure with the RMSE of a no change extrapolation. The RMSE of monthly predictions of the money multiplier in the 1962-65 period was .0151, which was 53 per cent as large as the RMSE for a no change extrapolation. In the 1966-69 period the RMSE was .0200, which was 64 per cent as large as the RMSE for a no change extrapolation.

Error-Response Mechanism

Once there is a possibility of error in money stock control, specification of an optimal operating strategy for changing the net source base requires that the money managers’ loss function be specified. There are many possible loss functions, each one representing somewhat different preferences by the policymakers. In our procedure a quadratic loss function of the following form is specified:

\[ L = (M - M^d)^2 \]

money manager’s loss function

where:

- \( M = mB \), actual money
- \( B = \) net source base
- \( M^d = \) desired money stock in period \( t \)

In the above expression the product of the money multiplier \( m \) and the net source base \( B \) gives the level of money achieved in period \( t \) by our operating procedure. \( M^d \) is the level of money consistent with a given desired growth rate of money. This type of loss function assigns proportionally more weight to large deviations of controlled money from desired than to smaller deviations.

Once the money manager’s loss function has been specified, the optimal strategy with respect to the net source base is the one that minimizes the expected value of the loss function. The expected value \( (E) \) is used to denote an expected value for this loss function may be written:

\[ E(L) = B^2 \text{ var } (m_i) + [M^d - BE(m_i)]^2 \]

Minimizing with respect to \( B \), gives the following expression for the optimal net source base \( (B^*) \):

\[ B^* = E(m_i) \left[ \frac{1}{1 + \text{ var } (m_i) / [E(m_i)]^2} \right] \]

To calculate the value for \( B^* \) in any period \( t \), (1) we used \( M^d \) in period \( t \), which is determined by the desired growth rate; (2) we used \( E(m_i) = \) predicted multiplier in period \( t \); and (3) \( \text{ var } (m_i) \) was approximated by taking the sum of squared residuals for the multiplier equation and dividing by 36 - \( K \cdot 1 \), where \( K \) equals 14, the number of independent variables in the forecasting equation for the multiplier.

Confidence Intervals for GNP

Projections with Money Stock Control

If a forecasting equation is used in which the money stock is assumed to be controlled by some procedure, then it is necessary to modify the standard error of forecast statistic associated with the forecasting equation. The importance of errors in money stock control can then be assessed by comparing the SEF of the GNP forecasting equation when there are no errors in money stock control with the standard error of forecast statistic \( (SEF^*) \) of GNP estimates when there are errors in money stock control.

One statistic frequently used by economists to assess the forecasting ability of an economic model is the standard error of estimate (SEE). However, a more appropriate measure of the forecasting ability of a model is the correctly specified standard error of forecast (SEF) statistic. The value of the SEF statistic depends upon the values assumed by the independent variables during the forecast period, and upon the variances and covariances of the parameters of the forecasting equation, as well as upon the SEE statistic.

In this section, the SEF statistic which is appropriate for our policy procedure is presented and a comparison of it with the SEE which assumes perfect money stock control is no longer appropriate. This SEF statistic could be too large or too small. In other words, policymakers should not use this statistic to construct the confidence interval for their GNP forecasts. The probability of over- or underestimating GNP could be greater or smaller than that indicated by this SEF statistic.

\[ \text{SEF} = \Delta M_{t+n} - \Delta M_{t+n} \pm \theta_{t+n} \]

where \( \theta_{t+n} \) is an error term.

With errors in the money stock control procedure, an SEF which assumes perfect money stock control is no longer appropriate. This SEF statistic could be too large or too small. In other words, policymakers should not use this statistic to construct the confidence interval for their GNP forecasts. The probability of over- or underestimating GNP could be greater or smaller than that indicated by this SEF statistic.

For a discussion of this subject, see Carl Christ, Econometric Methods and Models, John Wiley Co., 1968, pp. 549-564.

The derivation of the SEF statistic is presented in the technical appendices available as Working Paper No. 14.

For example, if the forecasting equation for the money multiplier results in an overestimate of the money multiplier (which results in the actual money stock being less than the desired), and if, in addition, the A-J equation overestimates the effect of a change in the money stock on GNP, then the influences of the two errors (negative correlation) tend to offset one another. However, when the errors in predicting the money stock and forecasting GNP are in the same direction (positive correlation), then the errors reinforce one another, and the error in GNP forecasts is increased.
The standard error of forecast statistic (SEF*) for the A-J equation, assuming errors in money stock control, is given by:

$$\text{SEF*} = \sqrt{(\text{SEF})^2 + \beta_1^2 \text{var}(\tilde{\epsilon} + \epsilon) + 2 \beta_1 \text{cov}(\tilde{\epsilon} + \epsilon, \epsilon + \tilde{\epsilon})}$$

where: SEF denotes the standard error of forecast statistic when there are no errors in money stock control, and $\beta_1$ is the coefficient for contemporaneous changes in the money stock in the GNP equation.

Examining the expression for SEF*, it can be seen that the existence of errors in money stock control introduces two extra terms in the standard error of forecast statistic, involving the error in the money stock control procedure ($\tilde{\epsilon} + \epsilon$) and the error in the GNP equation ($\epsilon + \tilde{\epsilon}$). Terms with the variance ($\text{var}(\tilde{\epsilon} + \epsilon)$) and the covariance ($\text{cov}(\tilde{\epsilon} + \epsilon, \epsilon + \tilde{\epsilon})$) are introduced. Since in general these terms are not equal to zero, SEF* is unequal to SEF. As remarked earlier, the cov ($\tilde{\epsilon} + \epsilon, \epsilon + \tilde{\epsilon}$) may be either positive or negative. If it is positive, then this factor would increase the SEF*, if negative, it might be large enough to make SEF* less than SEF.32

Standard error of forecast statistics are dependent upon the particular values of the independent variables which apply to the prediction period. In particular, an SEF statistic assumes its absolute minimum value when the respective independent variables which enter into it take on values that equal their sample means. All other sets of values of the independent variables will generate larger values of the SEF statistic. The reason for this result resides in the statistical uncertainty surrounding the regression estimates of the coefficients in the forecasting equation.

For the period I-1953 - II-1969, the minimum SEF of the GNP equation is $3.87 billion. As an illustration of how the SEF statistic actually differs in practice from its minimum value, let us consider the hypothetical problem of predicting GNP for each of the four quarters of 1970. Under conditions of perfect money stock control, the SEF statistic would assume the values given in row A of Table VI which are from approximately 7 to 14 percent larger (row B) than the minimum value of the SEF statistic.

For the money stock control procedure, the SEF* statistics are given in rows C and F of Table VI. The SEF* statistics in row C correspond to the quarterly average of the monthy money stock control procedure in the simulations with the GNP equation. The SEF* statistics in row F correspond to a quarterly money stock control procedure, and are rigorous "outer bounds" to the SEF* statistics given in row C.33

<table>
<thead>
<tr>
<th>Table VI</th>
<th>Standard Errors of Forecast</th>
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<tr>
<td></td>
<td>For the GNP Equation for 1970*</td>
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<td>(Dollar Amounts in Billions)</td>
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<tr>
<td>SEF with no error in money stock control</td>
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<tr>
<td>Percent increase of A over minimum SEF of A</td>
<td>B</td>
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<tr>
<td>SEF* with error in money stock control</td>
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<tr>
<td>$\text{simvar}(\tilde{\epsilon})$ and $\text{simcov}(\tilde{\epsilon}, \epsilon)$</td>
<td>C</td>
</tr>
<tr>
<td>Percentage increase of $\epsilon$ over $A$</td>
<td>D</td>
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<tr>
<td>Ratio of B to D</td>
<td>E</td>
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<tr>
<td>SEF* with error in money stock control</td>
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<tr>
<td>$\text{simvar}(\tilde{\epsilon})$ and $\text{simcov}(\tilde{\epsilon}, \epsilon)$</td>
<td>F</td>
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<tr>
<td>Percentage increase of $\epsilon$ over $A$</td>
<td>G</td>
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<tr>
<td>Ratio of B to G</td>
<td>H</td>
</tr>
</tbody>
</table>

where:
1. variance ($\epsilon_2$) = 14,749 (corresponds to SEE of 3,840)
2. simulation variance ($\text{simvar}(\tilde{\epsilon})$) = 0.674
3. simulation covariance ($\text{simcov}(\tilde{\epsilon}, \epsilon)$) = 0.011
4. equation variance ($\text{var}(\tilde{\epsilon})$): $\text{var}(\tilde{\epsilon}) = (\text{SEE}^2 + \text{SEE}_1^2)$
5. GNP equation is the A-J equation (sample period I-1953 to IV/1969)

The SEF* statistics associated with our monthly money stock control procedure are only 3 per cent larger than the SEF statistics assuming no errors in money stock control (see row D). To further understand the implications, probably the most reasonable estimate for the variance in money stock control, given that a monthly money stock control model is used in conjunction with a quarterly forecasting model of GNP. Unfortunately, the statistic simulation var($\epsilon$), makes no allowance for the imprecision in the coefficients of the multiplier forecasting equation. However, as shown in the technical appendices, this shortcoming can be overcome if the quarterly money stock control procedure is used. In that case, the equation var($\epsilon$) equals $\beta_1^2 \times (\text{SEE})^2$ (quarterly multiplier equation) which is the most appropriate estimate of var($\epsilon$). This variance is just the square of the lagged level of the base times the squared standard error of forecast of the multiplier forecasting equation.
tions of the standard errors of forecast in Table VI, it is
helpful to refer back to Table V on page 17. The data in
Table V show that the errors in money stock control have
a negligible effect on the policymaker’s ability to forecast
GNP, if 95 per cent confidence intervals are used as
standards of comparison.$^{24}$

$^{24}$ An illustration of how the confidence intervals in Table V
were computed is given below. Consider the perfect money
stock control case given in the first quarter of 1970 entry in
row A of Table VI, SEF = $4.143 billion. Because the
effects in predicting changes in GNP can be shown to be
normally distributed for large samples (see the technical
appendices in Working Paper No. 14), it is appropriate to
set up confidence intervals, using a table of the standard
normal distribution. A range of ±1.96 standard deviations
gives a 95 per cent confidence interval for the standard
normal distribution, whose standard deviation is unity by
definition.

Consequently, the distribution of normally distributed
errors with an SEF value of $4.143 has a proportionately
larger 95 per cent confidence interval of ± (1.96) X
(4.143) equals ± $8,120. When errors in money stock con-
trol raise the value of the SEF statistic to $4.267 (row C),
the probability of achieving the same confidence interval of
± $8,120 billion is reduced to 94.26 per cent, since now
only ± 1.90 standard deviations of the standard normal
distribution will give that same confidence interval,

\[ \pm (1.90) \times (4.267) \text{ equals } \pm 8,120. \]

For a comparison of 90 and 80 per cent confidence intervals
see the technical appendices available in Working Paper
No. 14.

This article is available as Reprint No. 72.