An Elementary Model of VC Financing and Growth

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Abstract

This article uses an endogenous growth model to study how the improvements in financing for innovative start-ups brought by venture capital (VC) affect firm innovation and growth. Partial equilibrium results show how lending contracts change as financing efficiency improves, while general equilibrium results show that better screening and development of projects by VC investors leads to higher aggregate productivity growth.

JEL codes: E13, E22, G24, L26, O16, O31, O40

1. INTRODUCTION

There is a strong link between venture capital (VC) financing and firm growth. Akcigit et al. (2019) show that companies with VC financing grow faster over time than companies using other sources of financing. Greenwood, Han, and Sánchez (2022b) show that in the first years after going public, VC-backed firms have employment and sales growth higher (5 and 7 percent, respectively) than publicly traded firms that did not receive VC financing. These authors also show that a connection exists between VC financing and innovation by demonstrating that VC investment increases the number of patents that a firm will file in the following years: a 10 percent increase in VC funding will induce a 7.9 percent increase in the numbers of patents expected by the firm in the three years after funding.

There is also evidence suggesting that VC financing is important for aggregate economic growth. Greenwood, Han, and Sánchez (2022a) build a model in which financing occurs through an optimal contract similar to Bergemann and Hege (1998), Clementi and Hopenhayn (2006), and Cole, Greenwood, and Sánchez (2016). The authors then embed the VC contract in a Romer (1986)-style model of endogenous growth to analyze the connection between VC financing and economic growth. The complexity of the dynamic contracting problem forces the analysis of the link between financing efficiency and productivity that is performed mainly with the numerical solution of the model. Quantitative results performed with a model calibrated to the US economy suggest that debasing VC financing would reduce the economy’s growth rate by almost 20 percent (from 1.8 percent to 1.5 percent).

This article aims to expand the analysis of the relationship between VC financing and growth by presenting a simpler model of VC financing and investigating how VC activity affects innovation and economic growth. The results demonstrate that more efficient VC financing—due to improvements in either project screening or development—increases both the probability that new projects are successfully developed and the share of the value of the project that the entrepreneur keeps. This same improvement in VC financing encourages...
entrepreneurs to choose a more innovative project. In turn, these results imply that on a balanced growth path, more efficient VC financing leads to a higher productivity growth rate.

2. SETUP

There are good and bad projects in this economy, and only good projects can become successful. The share of good projects is \( \rho \). An entrepreneur starts a project (or an idea) of productivity \( x \) in an economy with average productivity \( X \) that is growing at the rate \( g \). The research cost for an idea of productivity \( x \) is \( R(x,X) \), which is an increasing and convex function of how far the new idea is from average productivity \( X \) (which will be defined later). To obtain a closed-form solution, the research and development (R&D) cost function \( R \) is assumed to follow the functional form of

\[
R(x,X) = \frac{1}{x} \left( \frac{x}{X} \right)^t, \quad t > 2,
\]

where \( x/X \) is the step size of innovation or \( g \).

Successful firms with a project of productivity \( x \) use labor \( l \), capital \( k \), and the following technology to produce and maximize profits:

\[
S(x,X) = \max_{k,l} \{ x^\alpha l^{1-\alpha-\zeta} - lw(X) - rl \},
\]

taking as given wages \( w \) and the interest rate \( r \). While the interest rate, \( r \), is endogenously determined in Greenwood, Han, and Sánchez (2022a) by the economy’s growth rate, here we make the simplifying assumption that they are constant.

Note that \( S \) depends on aggregate productivity \( X \) because wages are a function of aggregate productivity. The surplus they obtain in a particular period is given by

\[
S(x,X) = x \zeta \left[ \left( \frac{\alpha}{\tau} \right)^\alpha \left( \frac{1-\alpha-\zeta}{w(X)} \right)^{1-\alpha-\zeta} \right]^{1/\zeta}.
\]

Using the expression for profits, the value of a successful project is given by the discounted sum of future profits,

\[
I(x;X,g_w) = \sum_{i=1}^\infty (s\delta)^{i-1} S(x,w_{g_w}^{i-1}),
\]

\[
= \frac{x}{w(X)^{(1-\alpha-\zeta)/\zeta}} \sum_{i=1}^\infty (s\delta)^{i-1} \zeta \left[ \left( \frac{\alpha}{\tau} \right)^\alpha \left( \frac{1-\alpha-\zeta}{g_w^{i-1}} \right)^{1-\alpha-\zeta} \right]^{1/\zeta},
\]

where \( s \) is the probability that the project survives to the next period, \( \delta \) is the rate at which the entrepreneurs discount the future, and \( g_w \) is the growth rate of wages. Dividing and multiplying by \( X \) and referring to a large term that depends on several parameters and the endogenous growth rate of wages as \( \Gamma(g_w) \), the value of an initial public offering (IPO) can be rewritten as

\[
I(x;X,g_w) = \frac{x}{X} \frac{X}{w(X)^{(1-\alpha-\zeta)/\zeta}} \sum_{i=1}^\infty (s\delta)^{i-1} \zeta \left[ \left( \frac{\alpha}{\tau} \right)^\alpha \left( \frac{1-\alpha-\zeta}{g_w^{i-1}} \right)^{1-\alpha-\zeta} \right]^{1/\zeta},
\]

\[
= g_w \frac{x}{w(X)^{(1-\alpha-\zeta)/\zeta}} \Gamma(g_w),
\]

where the firm will take the term \( \Gamma(g_w) \) as given at the time of selecting the size of innovation, \( g \), which is equal to \( x/X \).

3. PRODUCTIVITY AND LABOR MARKET EQUILIBRIUM

To obtain average productivity (i.e., \( X \)), we sum across the productivity of all firms and divide it by the number of firms. The number of entrants is constant and equal to \( n \),¹ and the number of firms of age 1 with productivity

¹. In Greenwood, Han, and Sánchez (2022a), the number of entrants is endogenously determined as a function of the expected profits of becoming an entrepreneur.
Another way of obtaining the sum of productivity across all firms is by multiplying the number of firms $N = 1/\alpha$ by average productivity $X$; that is, $N \cdot X$. Combining these two expressions, we obtain

$$X = x_{-1} \frac{1 - s}{1 - s/g_x},$$

where we recall that $x_{-1}$ is given but $g_x$ is the key variable that will be determined in the equilibrium of the model.

Labor demand for a project with productivity $x$ is

$$l(x, w) = x \left[ \left( \frac{\alpha}{\tau} \right)^\alpha \left( \frac{1 - x - \zeta}{w} \right)^{1 - \alpha} \right]^{1/\zeta}.$$

Hence, we can write the labor-market-clearing condition by adding the labor demand of all firms and setting it equal to the aggregate labor supply, which is assumed to be 1:

$$\left[ \left( \frac{\alpha}{\tau} \right)^\alpha \left( \frac{1 - x - \zeta}{w} \right)^{1 - \alpha} \right]^{1/\zeta} x_{-1} n (1 + s/g_x + (s/g_x)^2 + ...) = 1$$

or

$$\left[ \left( \frac{\alpha}{\tau} \right)^\alpha \left( \frac{1 - x - \zeta}{w} \right)^{1 - \alpha} \right]^{1/\zeta} x_{-1} n \frac{1 - s}{1 - s/g_x} = 1.$$

Since the last term is very close to average productivity, we can use this equation to solve for $w$ as a function of $X$ and parameters:

$$w(X) = \left( \frac{\alpha}{\tau} \right)^{\alpha/(1-\alpha)} \frac{1 - x - \zeta}{1 - \alpha - \zeta} \left( \frac{x_{-1}}{1 - s/g_x} \right)^{\zeta/(1-\alpha)}$$

$$= \left( \frac{\alpha}{\tau} \right)^{\alpha/(1-\alpha)} \frac{1 - x - \zeta}{1 - \alpha - \zeta} \left( \frac{n}{1 - s} \right)^{\zeta/(1-\alpha)}$$

$$= B \times \left( \frac{n}{1 - s} \right)^{\zeta/(1-\alpha)},$$

where $B = \left( \frac{\alpha}{\tau} \right)^{\alpha/(1-\alpha)} (1 - \alpha - \zeta)$.

### 4. VC CONTRACT

Though equipped with ideas, the entrepreneurs have no money, so they must seek financing from VC investors. Both the entrepreneur and the investors discount future payoffs at the rate $\delta$. If the project becomes successful and can start producing in the next period, the value of the project is $I(x; X, g_x)$, which is the discounted sum of future profits. The probability for a project to succeed ($\sigma$) hinges on the amount of money spent on developing the project, $D(\sigma)$. Since a higher success probability implies a higher cost, the development cost function $D(\sigma)$ is assumed to be increasing and convex in $\sigma$. VC investors will choose $\sigma$ when deciding how much to spend on developing the project. In return for financing the project, they ask for a share $\epsilon$ of the projects value when the project succeeds. They can also detect a share $\beta$ of the bad projects, which they shut down. Thus, $\beta$ is a measure of the evaluation efficiency of the VC industry.

The VC industry is modeled as a competitive industry, so the contract is written to maximize the entrepreneurs’ payoff. From the perspective of the entrepreneurs, the expected value of starting a project with VC financing is

$$C(x; X, g_x) = \max_{(\sigma, \epsilon) \in [0,1]^2} \delta \rho \sigma [I(x; X, g_x) \cdot (1 - \epsilon)],$$

where $x_{-1}$ is the productivity where the idea was generated one period ago. We assume that it takes one period to materialize the idea (if it is good).
subject to
\[
0 = \underbrace{\epsilon \rho \delta I(x; g_x X, g_w)}_{\text{Revenue from successful projects}} - \underbrace{w(X) R(x, X) - [\rho + (1 - \beta)(1 - \rho)] w(X) D(\sigma)}_{\text{Financing cost}}.
\]

The function \( C(x; X, g_w) \) describes the value the entrepreneur will receive if the project is good and successful, which occurs with probability \( \rho \sigma \). Note that what the entrepreneur receives is a share \((1 - \epsilon)\) of the value of the IPO, \( I(x; g_x X, g_w) \), which was described above. Also note that the other part of the IPO’s value is received by the VC investor and is therefore part of the zero-profit constraint (i.e., \( \rho \sigma I(x; g_x X, g_w) \)). However, the investors are facing two types of expenses: they will cover the research expenses for all projects as well as the development cost for projects remaining in the funding pool (i.e., all good projects and the bad ones that are not shut down).\(^3\) Recall that the evaluation efficiency of VC is not perfect, so they detect only a share \( \beta \) of the bad projects.\(^4\)

Note also that the maximization problem is precisely the same as a problem where entrepreneurs maximize their profits by spending the R&D costs by themselves (if entrepreneurs and banks have the same ability to select and develop projects). This means that the result will not change if only one decision maker decides on the success probability and firms’ innovation.

To obtain the optimal solution for the characteristics of the contract, \((\sigma^*, \epsilon^*)\), we derive their first-order conditions (FOCs):
\[
\rho \delta I(x; g_x X, g_w) (1 - \epsilon) + \lambda \rho \delta I(x; g_x X, g_w) \epsilon - \lambda [\rho + (1 - \beta)(1 - \rho)] w(X) D'(\sigma) = 0, \quad (\sigma)
\]
and
\[
-\rho \delta \sigma I(x; g_x X, g_w) + \lambda \rho \delta \sigma I(x; g_x X, g_w) = 0, \quad (\epsilon)
\]
where \( \lambda \) is the multiplier associated with the above problem. The optimal solution for \( \epsilon \) comes from the zero-profit constraint. An intuitive expression emerges for the equity share of the VC investors, as follows:
\[
\epsilon = \frac{[\rho + (1 - \beta)(1 - \rho)] w(X) D(\sigma) + wR(x, X)}{\rho \delta \sigma I(x; g_x X, g_w)} = \frac{\text{expenses}}{\text{expected discounted profits}}.
\]

The FOC for \( \epsilon \) gives an expression for the Lagrange multiplier, \( \lambda = 1 \). In addition, combining the FOC for \( \sigma \) with the expression for the Lagrange multiplier, we can obtain the following intuitive expression for the optimal choice of \( \sigma \):
\[
[\rho + (1 - \beta)(1 - \rho)] w(X) D'(\sigma) = \frac{\rho \delta I(x; g_x X, g_w)}{\sigma, \text{ marginal cost}} \sigma, \text{ marginal benefit}
\]

To derive an analytical solution, the development cost function \( D \) is assumed to follow the functional form of
\[
D(\sigma) = \frac{\sigma^2}{2z_D},
\]
where \( z_D \) is the efficiency of VC in developing projects.\(^5\) This implies that \( D'(\sigma) = \frac{\sigma}{z_D} \). Using this in the efficiency for \( \sigma \) yields
\[
\sigma^* = \frac{z_D \rho \delta I(x; g_x X, g_w)}{w(X) [1 - \beta (1 - \rho)]}.
\]

This expression for \( \sigma^* \) delivers the first set of results taking as given aggregate variables \( X \) and \( g_w \) (i.e., in partial equilibrium).

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3. Note that both the R&D cost \( (R) \) and the development cost \( (D) \) are expressed in terms of labor. Hence, both terms are multiplied by the wage rate \( (w) \) in the zero-profit constraint.
4. While the contract here is a one-period interaction between the VC investor and the entrepreneur, Greenwood, Han, and Sánchez (2022a) analyze a multiperiod version of this problem that also incorporates moral hazard.
5. We can also derive an analytical solution with a more general form of cost function \( D(\sigma) = \sigma^u / u z_D \) \((u > 1)\). In this case, the necessary condition for \( \tau \) is \( \tau > w/(n - 1) \) instead of \( \tau > 2 \).
**Lemma 1:** The probability for a successful project to succeed ($\sigma^*$) is increasing in the following:
- the efficiency of VC investors to detect bad projects, $\beta$
- the efficiency of VC investors to lend expertise to entrepreneurs, $z_D$
- the share of good projects, $\rho$
- the value of the project, $I$

The results of Lemma 1 are very intuitive. As either the cost of financing declines (higher values of $\beta$ or $z_D$) or the project’s quality improves (higher $\rho$ or $I$), it is more likely that a project financed by a VC investor succeeds.

Substituting the solution for $\sigma^*$ into the expression for $\epsilon$, we obtain
$$\epsilon^* = \frac{1}{2} + \frac{w(X)^2 [1 - \beta (1 - \rho)] R(x, X)}{z_D (\rho \delta I(x; g, X, g_w))^2}.$$  

Interestingly, note that there is an upper bound value of $x$ that can be financed because $\epsilon^* \leq 1$. With this expression at hand, we can derive the second set of partial equilibrium results as follows.

**Lemma 2:** The VC investors’ share of equity, $\epsilon^*$, is decreasing in the following:
- the evaluation efficiency of VC investors to detect bad projects, $\beta$
- the development efficiency of VC investors to lend expertise to entrepreneurs, $z_D$
- the share of good projects, $\rho$
- the value of the project, $I$

To understand the results in Lemma 2, recall that VC is modeled as a competitive industry. Hence, a higher level of VC efficiency (higher $\beta$ or $z_D$) contributes to lower levels of VC expenses, and thus the VC investors can break even when their share of equity is at a lower level. Analogously, since the investors are chasing the same pool of projects, competition among them will transfer the surplus associated with better quality of projects (higher $\rho$ or $I$) to the entrepreneurs, whereas the VC investors end up with a lower share of equity in equilibrium.

### 5. INNOVATION CHOICE

The choice of the step size for innovation is made by an entrepreneur choosing $x$ to maximize its payoff; that is,
$$V(X, g_x) = \max_x C(x; X, g_w).$$

With the solutions for ($\sigma^*, \epsilon^*$) and the expression for the value of a successful project $I(x; g, X, g_w)$, we can rewrite $C(x, X, g_w)$ in terms of the step size for innovation, $g = x/X$:
$$C(x, X, g_w) = \delta \rho \sigma^* I(x; g, X, g_w) (1 - \epsilon^*),$$
$$= g^2 \left( \frac{X}{w(g_x X)^{1 - \epsilon^*}} \right)^2 \frac{z_D (\rho \delta)^2 \Gamma(g_w)^2}{2w(X) [1 - \beta (1 - \rho)]} - \frac{w(X)}{z_R} g^{t-1}.$$  

To find the optimal step size of an innovation, we compute the FOC with respect to $g$:
$$g \left( \frac{X}{w(g_x X)^{1 - \epsilon^*}} \right)^2 \frac{z_D (\delta \rho \Gamma(g_w))^2}{w(X) [1 - \beta (1 - \rho)]} - \frac{w(X)}{z_R} g^{t-1} = 0.$$  

Solving gives the step size of innovation chosen by the entrepreneur:
$$g^* = \left( \frac{z_R z_D (\delta \rho \Gamma(g_w))^2}{(1 - \beta (1 - \rho)) w(X)^2} \left( \frac{X}{w(g_x X)^{1 - \epsilon^*}} \right)^2 \right)^{1/(t-2)}.$$  

This solution is now used to derive the following partial equilibrium results about the optimal step size of innovation.
Lemma 3: The step size of innovation, $g^*$, is increasing in
- the evaluation efficiency of VC investors to detect bad projects, $\beta$;
- the development efficiency of VC investors to lend expertise to entrepreneurs, $z_D$;
- the share of good projects, $\rho$;
and it is decreasing in the growth rate of wages, $g_w$, which the entrepreneur takes as given.

Recall that entrepreneurs choose how innovative (how far ahead of the pack) their project is by considering alternative values of $g$ given the aggregate conditions of the economy. Intuitively, Lemma 3 suggests that more efficient VC financing (higher $\beta$ and $z_D$) and a better pool of projects (higher $\rho$) encourage an entrepreneur to choose a more innovative project. Finally, the last result relates the choice of innovation to the aggregate conditions of the economy. In particular, it indicates that the entrepreneurs will choose less innovative projects when the wage rate grows faster because growing wages erodes the expected profits from the project.

6. ECONOMIC GROWTH

We can embed this VC contract into a growth model as long as the economy is growing at a constant rate. In particular, the next lemma demonstrates that along a balanced growth path, the contract’s characteristics and the innovation choice will be constant over time.

Lemma 4: There is a balanced growth path where the following are constant: the growth rate of wages, $g_w = \frac{x}{X}$; the equity share of entrepreneurs, $e^*$; the probability for a good project to succeed, $\sigma^*$; and the step size of innovation, $g^*$.

So far we have taken the choice of innovation by entrepreneurs, $g$, and the growth of average productivity in the economy, $g_x$, as two different things. To ensure we have an equilibrium, we find a growth rate of average productivity consistent with the choice of innovation, $g$. This consistency can be obtained by pinpointing the relationship between $g_x$ and $g$. In particular, note that the growth rate of productivity is

$$g_x = \frac{X'}{X} = \frac{x'}{x}$$

and that $g = x/X$. Therefore, a link between aggregate productivity growth, $g_x$, and the step size of innovation, $g$, can be established as follows:

$$g_x = \frac{x}{x-1} = \frac{gX}{x-1} = g \frac{1-s}{1-s} g_x.$$

This provides an expression for $g$ as a function of $g_x$:

$$g = \frac{g_x - s}{1-s}.$$

In addition, the consistency between the growth rate of wages, $g_w$, and aggregate productivity growth, $g_x$, is also key to ensuring the existence of an equilibrium. A link between $g_w$ and $g_x$ is written as

$$g_w = \frac{w'}{w} = \left(\frac{X'}{X}\right)^{\frac{1-s}{\alpha}} = g_x^{\frac{r}{1-s}}.$$

We will use this relationship between $g$, $g_w$, and $g_x$ in the solution of $g^*$ to find the equilibrium growth rate of the economy. But first we need to rewrite $g^*$ as a function of $g_x$. We start by substituting $\Gamma(w)$ in the expression for $g^*$, which is referred to as $g$ for simplicity:

$$g = \left(\frac{\delta \rho}{w(X)} \left(\frac{z_R z_D}{1-\beta(1-\rho)}\right)\right)^{1/2} \frac{X}{w(g_x X)^{(1-\alpha-\zeta)}} \sum_{t=1}^{\infty} \left(\frac{s\delta}{g_w}\right)^{(1-\alpha-\zeta)/\zeta} (1-s) (1-\alpha-\zeta) \left(\frac{s\delta}{g_w}\right)^{(1-\alpha-\zeta)/\zeta} \right)^{2/(t-2)} \times A,$$

where

$$A = \left(\frac{\zeta}{\alpha} \right)^{\frac{\alpha}{\zeta}} \left(1-\alpha-\zeta\right)^{2/(t-2)}.$$
Replacing \( w(X) \) and solving the series for \( g_w \),

\[
g = \left( \delta \rho \left( \frac{z_R z_D}{\tilde{t}[1 - \beta(1 - \rho)]} \right)^{1/2} \left( \frac{1 - s}{n} \right) \left( \frac{1}{g_w} \right)^{(1 - \alpha)/(1 - \alpha)} \right)^{2/(1 - 2)} \times \hat{A},
\]

where \( \hat{A} = A/B^{(1 - \alpha)/(1 - 2)} \) for the value of \( B \) defined above.

Now we need to use the expressions for \( g, X, g_w \) to find an equation for \( g_x \). We obtain

\[
\frac{g_x - s}{1 - s} = \hat{A} x
\]

To gain more intuition from this equation, let

\[
\Gamma = \left( \delta \rho \left( \frac{z_R z_D}{\tilde{t}[1 - \beta(1 - \rho)]} \right)^{1/2} \left( \frac{1 - s}{n} \right) \left( \frac{1}{g_w} \right)^{(1 - \alpha)/(1 - \alpha)} \right)^{2/(1 - 2)} \times \hat{A}.
\]

It transpires that \( \Gamma \) is increasing in research efficiency \( (z_R) \), VC investors' development efficiency \( (z_D) \), VC investors' evaluation efficiency \( (\beta) \), and the share of good ideas \( (\rho) \).

\( \Gamma \) is useful to rewrite the equation for \( g_x \) as

\[
\frac{g_x - s}{1 - s} = \Gamma \times \left( \frac{1 - s}{g_w} \right)^{(1 - \alpha)/(1 - \alpha) - s\delta})^{2/(1 - 2)}.
\]

In light of this, to understand the impact of the efficiency of VC financing, the quality of the projects, and the R&D efficiency on the growth of the general model, we just need to figure out the impact of \( \Gamma \) on \( g_x \).\(^6\) The results are summarized in the next lemma.

**Lemma 5:** The equilibrium growth rate of productivity in the economy, \( g_x \), is increasing in the following:

- the evaluation efficiency of VC investors to detect bad projects, \( \beta \)
- the development efficiency of VC investors to lend expertise to entrepreneurs, \( z_D \)
- the share of good projects, \( \rho \)
- the efficiency of R&D, \( z_R \)

Finally, we check that there indeed exists a balanced growth path. It will be shown that \( \{x^*, w^*\} \), which is the solution for the old problem, solves the new one for \( x^* = g_x x \) and \( X^* = g_x X \). First, observe that if \( x' = g_x x \) and \( X' = g_x X \), then \( I(x'; X', g_w) = g_w I(x; X, g_w) \). This can be seen because \( x \) will rise by \( g_x \) and wages by \( g_w \). Then, it is immediate that \( C(x'; X', g_w) = g_w C(x; X, g_w) \). Now, consider the zero-profit constraint. At the conjectured solution, the right-hand side will inflate by the factor \( g_w \) since \( I(x'; X', g_w) = g_w I(x; X', g_w) \), \( w^* = g_w w^* \), and \( R(x'; X') = R(x, X) \). This is trivially true for the left-hand side. Hence, the zero-profit constraint holds at the new allocations.

To summarize, at the conjectured new solution, the objective function and the constraint scale up by the same factor of proportionality \( g_w \). By canceling out this factor of proportionality, the new problem reverts to the old one. Likewise, it is easy to deduce that if \( x \) solves the choice problem of the step size for \( X \), then \( x' = g_x x \) solves it when \( X' = g_x X \). This occurs because this problem also scales up by the factor of proportionality \( g_w \), and so \( V(X, g_x) \) will grow at the same rate as wages, \( w \). Additionally, \( g_x^* \) is constant since it does not depend on either \( x \) or \( X \). Therefore, there exists a balanced growth path where the growth rate of wages, \( g_w = g_x^{1/(1 - \alpha)} \).

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\(^6\) It is simple to see that if the \( \Gamma \) increases, the right-hand side increases, and that would then lead to an increase in \( g_x \) to increase the left-hand side and to reduce the right-hand side.
the equity share of entrepreneurs, $e^*$, the probability that a good project succeeds, $\sigma^*$, and the step size of innovation, $g^*$, are constant, as in Lemma 4.7.

Taking stock of all these lemmas, our findings have unveiled exactly how VC contributes to innovation and economic growth. To be specific, enhanced VC efficiency encourages VC investors to invest more in financing ventures (Lemma 1), and the entrepreneurs are rewarded with a larger share of the pie because of competition among the investors (Lemma 2). Consequently, the entrepreneurs are incentivized to pursue more radical innovations (Lemma 3), which contributes to a higher level of long-run productivity growth (Lemma 5).

7. CONCLUSION

This article explores the connection between VC financing and economic growth. It introduces a simple endogenous growth model with a VC financing contract along the lines of Greenwood, Han, and Sánchez (2022a). The emphasis is on the model’s simplicity and its analytical solutions that allow for a characterization of the model. The results describe how the VC activity changes as project screening and development improve and how this better financing affects aggregate productivity growth.

One of the crucial questions left unanswered is the role of VC financing to account for differences in development across countries. Although more research is needed in this area, the findings in Cole, Greenwood, and Sánchez (2016) and in Greenwood, Han, and Sánchez (2022a) suggest that differences in the cost of enforcing contracts, as well as the taxation of successful entrepreneurs, may be behind such cross-country differences.

REFERENCES


For the optimally chosen $g^x$, the VC investors’ share of equity, $e^*$, is written as $1/2 + 1/\iota$, which is only dependent on the convexity of the R&D cost function, $\iota$. Since $\iota$ is larger than 2 to have a general equilibrium, $e^*$ is less than 1. As such, the upper bound of $e (e \leq 1)$ does not matter if $g^x$ is optimally chosen.